

## **Bladder tissue biomechanical behavior: experimental tests and constitutive formulation**

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## **ABSTRACT**

A procedure for the constitutive analysis of bladder tissues mechanical behavior is provided, by using a coupled experimental and computational approach. The first step pertains to the design and development of mechanical tests on specimens from porcine bladders. The bladders have been harvested, and the specimens have been subjected to uniaxial cyclic tests at different strain rates along preferential directions, considering the distribution of tissue fibrous components. Experimental results showed the anisotropic, non-linear and time-dependent stress-strain behavior, due to tissue conformation with fibers distributed along preferential directions and their interaction phenomena with ground substance. In detail, experimental data showed a greater tissue stiffness along transversal direction. Viscous behavior was assessed by strain rate dependence of stress-strain curves and hysteretic phenomena. The second step pertains the development of a specific fiber-reinforced visco-hyperelastic constitutive model, in the light of bladder tissues structural conformation and experimental results. Constitutive parameters have been identified by minimizing the discrepancy between model and experimental data. The agreement between experimental and model results represent a term for evaluating the reliability of the constitutive models by means of the proposed operational procedure.

## **KEYWORDS:**

Bladder, soft tissue mechanics, experimental test, non-linear mechanics, computational approach.

## 1 INTRODUCTION

2 Lower urinary tract dysfunction affects about 400 million people worldwide because of  
3 mechanical, neurological or idiopathic insult. Different congenital or acquired pathologies  
4 determine anatomical and functional alterations also of the bladder-sphincteric apparatus with  
5 consequent impaired urinary continence (Korossis et al., 2009, Irwin et al., 2006, Sacco et al.,  
6 2006). An engineering approach can provide reliable tools for the treatments of pathologic  
7 situations, as to design the most appropriate long-term surgical repair procedures or to  
8 investigate and develop materials for bladder reconstruction.

9 The structural models of specific organs is addressed, by a computational approach, to the  
10 investigation of the mechanical response of biological tissue and structures in health and  
11 disease, also to analyze interaction phenomena with biomedical devices (Carniel et al., 2013;  
12 Carniel et al., 2014; Krywonos et al., 2010). The definition of computational models requires  
13 both 3D virtual solid models of anatomical region and reliable constitutive formulations of  
14 biological tissues. As matter of example, the three dimensional reconstruction of the pelvic  
15 district, as virtual solid models, by reverse engineering techniques has proved to be useful for  
16 preoperative planning, allowing to analyze the outcomes of different reconstructive solutions  
17 or to support diagnostic hypotheses (Chai et al., 2012; Hampel et al, 2004; Marino and  
18 Bignardi, 2002; Pel and van Mastrikt, 2007; Vlastelica et al., 2007). **The constitutive analysis  
19 of soft biological tissues mechanics is usually performed by a coupled experimental and  
20 computational approach. Mechanical tests must be accurately designed accounting for the  
21 expected tissue properties, considering anisotropic behavior, non-linear effects and time-  
22 dependent phenomena, evaluating the tissue structural configuration. The experimental  
23 results allows to provide the appropriate constitutive formulation and to identify the  
24 associated parameters.**

25 Different authors reported investigations about bladder tissues mechanics, with regard to both  
26 experimental and computational activities. Regnier et al. (1983) provided hyperelastic  
27 formulation to interpret the non-linear elastic behavior. Salinas et al. (1992) and Nagatomi et  
28 al. (2004) developed experimental activities to evaluate the viscoelastic properties together  
29 with preliminary model formulation. Van Mastriigt et al (1981) carried out an investigation of  
30 the strain rate dependence of the viscoelastic response of the urinary bladder wall. Korossis et  
31 al. (2009) and Chen et al. (2013) investigated the anisotropic and non-linear elastic behavior  
32 by experimental activities, considering also the relationship between the tissue histo-  
33 architecture and mechanical properties.

34 The improvement provided by the current study is the combined action of experimental and  
35 numerical approach for the analysis of the bladder tissue mechanics, aiming at a reciprocal  
36 reliability assessment. Specific experimental tests are developed and, considering histological  
37 configuration and experimental results, an appropriate constitutive model is implemented.

38 Some general notes are reported with regard to the histomorphometric configuration of the  
39 bladder tissue, aiming at the biomechanical characterization. The wall is a complex structure  
40 made up of mucosa, submucosa, muscularis and serosa layers as reported by different authors  
41 (Bouhout et al., 2013; Zanetti et al., 2012). The mucosa is the innermost tissue and consists of  
42 transitional epithelial cells layers, which adapt their shape to the bladder filling. The  
43 submucosa is a thick layer of loose connective tissue and it is rich in elastic fibers, nerve,  
44 blood and lymphatic vessels. The tunica muscularis is composed of three smooth muscular  
45 layers together with connective elements. Within the inner and the outer layers, muscular  
46 fibers are predominately distributed from the apex to the bottom of the bladder, while a  
47 circumferential organization characterizes the fibers within the middle layer. The serosa layer  
48 is a visceral peritoneum and the mechanical contribution to the wall stiffness and strength in  
49 almost negligible. With regard to the overall contribution of connective fibers, elastin

50 provides the recoiling mechanism of the tissues (Korossis et al. 2009), while collagen fibers  
51 are preferentially aligned along apex to base direction (Gilbert et al., 2009).  
52 Such a complex configuration, with particular regard to fibrous components, entails the  
53 anisotropic and non-linear behavior. Fibrous structures, as muscular and connective ones,  
54 undergo stiffening phenomena with stretch, leading to non-linear elastic properties. Micro-  
55 structural rearrangement phenomena, as fibers uncrimping and interaction with liquid  
56 components, lead to viscous effects (Bouhout et al., 2013; Korossis et al. 2009; Zanetti et al.,  
57 2012). Aiming at the mechanical characterization, tensile tests on tissue specimens are  
58 developed along different directions and at different strain rates. A constitutive formulations  
59 is developed in the framework of a theory that accounts for anisotropic behavior, coupled  
60 geometrical and material non-linearity and time-dependent phenomena. The identification of  
61 constitutive parameters is performed comparing model results and data from mechanical tests  
62 by fitting procedures. The reliability of constitutive formulation and parameters obtained is  
63 assessed by comparison of computational and experimental results with reference to  
64 additional experimental tests.

## 65 MATERIALS AND METHODS

### 66 Mechanical tests

67 The experimental tests have been performed on tissue specimens from pig bladder, because  
68 of the extensively supported similarity of pig and human tissues mechanics. Different authors  
69 (Dahms et al. 1998; Korossis et al. 2009) investigated bladder of different species, finding  
70 that pig and human bladder tissues show similar histomorphometric conformation and  
71 mechanical behavior. The intact bladders of three Large White pigs, that were 11-13 months  
72 old and about 160 Kg in weight, were collected from a local abattoir and transferred to the  
73 laboratory. The bladders were cleaned for luminal contents, adjacent tissues were dissected  
74 and the organs were frozen at -20°C. Twenty-four hours before testing, bladders were put  
75 into the fridge and completely defrosted (Dahms et al. 1998). They were dissected along the  
76 apex-to-base line, and samples were harvested from the lateral region of the wall. In detail,  
77 specimens were isolated using an I-shaped die cutter along apex-to-base (AB) direction and  
78 along transverse (T) direction (Figure 1). This shape prevented sample from over-stressing  
79 next to the grips, as witnessed by frequent failure in this area in the case of constant section  
80 specimens. Specimens were measured by means of photogrammetry to identify the central  
81 region and to evaluate width and thickness profiles using the image analysis software ImageJ  
82 (Zanetti et al. 2012). The number of specimens and their average width and thickness are  
83 reported in Table 1, while the length of each specimen in the central region of the I-shape was  
84 12 mm. The length of the specimen has been chosen in relation to the limits of the loading  
85 machine and in agreement with the efficacy of the experimental tests performed (Bose  
86 Electroforce® 3200; 225 N maximum force; 12 mm stroke; static to 300 Hz frequency  
87 response), considering a 100% strain was to be reached. After their isolation, specimens were  
88 stored in the fridge within glass tubes containing PBS for less than 10 h. During tests,  
89 samples were continuously dampened with the solution to keep them wet.

90 A Bose Electroforce® equipment was used to perform tensile tests on the tissue specimens.  
91 Because of preliminary evaluation of samples strength, a load cell with capacity of 200 N  
92 with accuracy of  $\pm 0.1\%$  was adopted. Clamping of the specimens was performed by grips (5  
93 mm length and 20 mm wide), according to an intensity of about 100 kPa, adjusted to avoid  
94 the slippage and the damage of the specimens. The slippage has been checked during tests  
95 looking at the overall trend in the force/displacement curve. At the end of tests, it was  
96 verified that the length of the specimen clamped remained unchanged, and that there were no  
97 marks of longitudinal slips. Force and displacement signals were synchronized by means of a  
98 trigger signal. The displacement sensor measured clamp-to-clamp displacement while the  
99 load cell was placed below the specimen in correspondence of the fixed end. The reference  
100 point for zero-displacement was obtained applying a force threshold equal to 0.1 N (Mavrilas  
101 et al., 2005). The test protocol accounted for a first test of stress relaxation followed by cyclic  
102 tests at different strain rates. The stress relaxation test was performed reaching a grip  
103 displacement of 12 mm (corresponding to an axial strain of 100%) with a strain rate of  
104 1.33%/s, followed by a 600 s holding time.  
105 Subsequently, cyclic tests were performed reaching a strain of about 50%. Loading and  
106 unloading steps were performed accounting for different strain rates, as 10, 50, 100, 200, 500  
107 %/s. The specific strain rates were defined considering results from constitutive  
108 investigations developed by other authors (Van Mastrigt et al., 1981; Salinas et al., 1992;  
109 Nagatomi et al., 2004). High strain rates, even overcoming physiological limits, support the  
110 overall analysis with regard to the constitutive formulation. In detail, such analyses led to  
111 relaxation times ranging between  $10^{-1}$  and  $10^1$  seconds and testing times were consequently  
112 defined.  
113 During tests, load and displacement were acquired from a load cell and a linear differential  
114 transformer, respectively. The signals were acquired at 2 kHz sampling frequency.

115 Accounting for the undeformed geometrical conformation of the experimental specimens,  
116 load versus displacement data were converted to nominal stress versus stretch data. The stress  
117 was defined according to the Lagrangian scheme as the ratio of load to unloading cross-sectional  
118 area, whereas the axial strain was defined as displacement referred to the initial specimen  
119 length that is the distance between fixtures (Dahms et al. 1998). Results from cyclic tests on  
120 tissue specimens were post-processed to identify average nominal stress-stretch curves and  
121 scatter bands.

122

### 123 **Constitutive formulation**

124 Conformation of bladder wall must be investigated to interpret the overall mechanical  
125 behavior. It must be pointed out, for example, that fact that submucosa and muscular layers  
126 mainly contribute to the wall stiffness and strength. Such layers are composed of fibrous  
127 structures, as collagen and elastin in submucosa and smooth muscular fibers in muscular  
128 layers, embedded within an isotropic ground matrix. With particular regard to muscular  
129 layers, fibers are locally distributed along two main preferential directions determining the  
130 anisotropic behavior. The conformation of fibers and the interaction phenomena with ground  
131 substance entail non-linear elasticity and time dependent phenomena (Natali et al. 2004). A  
132 visco-hyperelastic constitutive formulation is assumed to interpret the typical features of the  
133 tissue mechanical response. The model accounts for the following Helmholtz free energy  
134 function (Natali et al. 2010, 2011):

$$135 \quad \psi(\mathbf{C}, \mathbf{q}^i) = W^0(\mathbf{C}) - \sum_{i=1}^n \int_0^t \frac{1}{2} \mathbf{q}^i : \dot{\mathbf{C}} dt \quad (1)$$

136 where  $W^0$  is an hyperelastic potential that specifies the instantaneous response of the tissue,  
137 while  $\mathbf{C}$  is the right Cauchy-Green strain tensor. Viscous variables  $\mathbf{q}^i$  quantify the relaxation



138 of stress components during loading. Structural rearrangement mechanisms of tissue elements  
139 over time entail such relaxation phenomena.

140 The specific hyperelastic potential is defined accounting for formulations that already  
141 proved their reliability in the framework of soft tissues mechanics (Fontanella et al.,  
142 2012; Fontanella et al., 2013; Forestiero et al., 2014), recalling that the mechanical  
143 behavior is determined by the properties of ground matrix and fibers and, consequently,  
144 the strain energy function can be additively decomposed:

$$145 \quad W^0(\mathbf{C}) = W_m^0(\mathbf{C}) + W_f^0(\mathbf{C}, \mathbf{a}_0, \mathbf{b}_0) \quad (2)$$

146 where  $W_m$  and  $W_f$  refer to the ground matrix and fibers contributions, respectively, while  $\mathbf{a}_0$   
147 and  $\mathbf{b}_0$  provide the preferential directions of fibrous elements, along apex-to-base and  
148 transverse directions, respectively.

149 The high liquid content of ground matrix determines the typical almost incompressible  
150 behavior of soft biological tissues (Weiss et al., 1996), and the following formulation of the  
151 ground matrix hyperelastic term  $W_m^0$  is proposed (Natali et al., 2012):

$$152 \quad W_m^0(\mathbf{C}) = -p(I_3 - 1) + \tilde{W}_m^0(\tilde{I}_1) \quad (3)$$

$$153 \quad \tilde{W}_m^0(\tilde{I}_1) = [C_1/\alpha_1] \left\{ \exp[\alpha_1(\tilde{I}_1 - 3)] - 1 \right\} \quad (4)$$

154 where  $\tilde{I}_1$  is the first iso-volumetric invariant of the right Cauchy-Green strain tensor, as  
155  $\tilde{I}_1 = \text{tr}(I_3^{-1/3}\mathbf{C})$ , and  $I_3$  is the third invariant, as  $I_3 = \det(\mathbf{C})$ . The term  $p$  serves as a  
156 Lagrange multiplier to ensure the kinematic constraint of almost incompressible continuum.  
157 Constitutive parameter  $C_1$  specifies the tissue shear stiffness as  $G = 2C_1$ , while parameter  $\alpha_1$   
158 regulates the non-linearity of the shear response, with reference to experimental results.

159 The definition of fibers contribution has to account for fibers rearrangement phenomena with  
160 stretch. A specific exponential formulation is provided (Natali et al., 2012):

$$161 \quad W_f^0(\mathbf{C}, \mathbf{a}_0, \mathbf{b}_0) = W_{fAB}(I_4) + W_{fT}(I_6) \quad (5)$$

$$162 \quad W_{fAB}^0(I_4) = [C_4/\alpha_4^2] \{ \exp[\alpha_4(I_4 - 1)] - \alpha_4(I_4 - 1) - 1 \} \quad (6)$$

$$163 \quad W_{fT}^0(I_6) = [C_6/\alpha_6^2] \{ \exp[\alpha_6(I_6 - 1)] - \alpha_6(I_6 - 1) - 1 \} \quad (7)$$

164 where  $I_4$  and  $I_6$  are structural invariants that specify tissue stretch along directions  $\mathbf{a}_0$  and  
 165  $\mathbf{b}_0$ , respectively. The constitutive parameters  $C_4$  and  $C_6$  are constants that define the fibers  
 166 initial stiffness, while  $\alpha_4$  and  $\alpha_6$  depend on fibers stiffening with stretch. Once the  
 167 hyperelastic potentials have been specified, the stress-strain relationship can be computed  
 168 accounting for thermo-mechanics principles (Natali et al., 2010):

$$169 \quad \mathbf{P}(\mathbf{C}, \mathbf{q}^i) = 2\mathbf{F} \frac{\partial \psi(\mathbf{C}, \mathbf{q}^i)}{\partial \mathbf{C}} = \mathbf{P}^0(\mathbf{C}) - \sum_{i=1}^n \mathbf{q}^i \quad (8)$$

$$170 \quad \mathbf{P}^0(\mathbf{C}) = 2\mathbf{F} \frac{\partial W^0(\mathbf{C})}{\partial \mathbf{C}} \quad (9)$$

171 where  $\mathbf{P}$  is the first Piola-Kirchhoff stress tensor and  $\mathbf{F}$  is the deformation gradient.  
 172 Accounting for the proposed formulation of the strain energy function, the nominal stress  
 173 tensor contributions from the ground matrix and fibers families are defined as it follows:

$$174 \quad \mathbf{P}_m^0 = 2\mathbf{F} \partial W_m / \partial \mathbf{C} = -p\mathbf{F}^{-T} + C_1 \exp[\alpha_1(\tilde{I}_1 - 3)] (2J^{-2/3}\mathbf{F} - 2/3\tilde{I}_1\mathbf{F}^{-T}) \quad (10)$$

$$175 \quad \mathbf{P}_{fAB}^0 = 2\mathbf{F} \partial W_{fAB} / \partial \mathbf{C} = 2(C_4/\alpha_4) \{ \exp[\alpha_4(I_4 - 1)] - 1 \} \mathbf{F}(\mathbf{a}_0 \otimes \mathbf{a}_0) \quad (11)$$

$$176 \quad \mathbf{P}_{fT}^0 = 2\mathbf{F} \partial W_{fT} / \partial \mathbf{C} = 2(C_6/\alpha_6) \{ \exp[\alpha_6(I_6 - 1)] - 1 \} \mathbf{F}(\mathbf{b}_0 \otimes \mathbf{b}_0) \quad (12)$$

177 According to the mechanics of visco-elastic materials, differential equations are introduced to  
 178 specify the evolution of viscous variables:

$$179 \quad \dot{\mathbf{q}}_m + \frac{1}{\tau_m} \mathbf{q}_m = \frac{\gamma_m}{\tau_m} \mathbf{P}_m^0 \quad (13)$$

$$180 \quad \dot{\mathbf{q}}_{fAB} + \frac{1}{\tau_{fAB}} \mathbf{q}_{fAB} = \frac{\gamma_{fAB}}{\tau_{fAB}} \mathbf{P}_{fAB}^0 \quad (14)$$

$$181 \quad \dot{\mathbf{q}}_{fT} + \frac{1}{\tau_{fT}} \mathbf{q}_{fT} = \frac{\gamma_{fT}}{\tau_{fT}} \mathbf{P}_{fT}^0 \quad (15)$$

182 where  $\tau_m, \tau_{fAB}, \tau_{fT}$  are relaxation times, as measures of time for the viscous processes  
 183 development,  $\gamma_m, \gamma_{fAB}, \gamma_{fT}$  are relative stiffness defining the stiffness contribution of viscous  
 184 processes.

185

### 186 **Identification of constitutive parameters**

187 The identification of constitutive parameters was performed comparing model results and the  
 188 average curves from cyclic tests on tissue specimens at different strain rates. The shape  
 189 conformation of the experimental samples allows the assumption of an homogeneous  
 190 distribution of stress and stretch fields within the central region of the specimen.  
 191 Consequently, analytical models can be developed to interpret the experimental situations.  
 192 The models define the trends of nominal stress with stretch along both apex-to-base and  
 193 transverse directions. If directions 1, 2 and 3 are oriented respectively in apex-to-base,  
 194 transverse and thickness directions in bladder, for a uniaxial loading condition, the  
 195 deformation gradient can be assumed as a diagonal tensor with principal stretches  $\lambda_1, \lambda_2, \lambda_3$ .  
 196 In detail,  $\lambda_1, \lambda_2$  specify the imposed stretch conditions for uniaxial tests in apex-to-base or  
 197 transverse direction, respectively, while  $\lambda_3$  is the stretch in the thickness direction. Fibre  
 198 orientations  $\mathbf{a}_0$  and  $\mathbf{b}_0$  can be evaluated as:

$$199 \quad \mathbf{a}_0 = [1, 0, 0], \quad \mathbf{b}_0 = [0, 1, 0] \quad (16)$$

200 Accounting for the deformation gradient assumed and the orientation of fibres, the specific  
 201 formulations of nominal stress components can be evaluated. In detail, the analytical model  
 202 has to provide the stress component  $P_{11}^{mod}$  for an experimentally imposed stretch  $\lambda_1^{exp}$ , with  
 203 regard to tests developed along the apex-to-base direction, and the stress component  $P_{22}^{mod}$

204 for an experimentally imposed stretch  $\lambda_2^{\text{exp}}$ , with regard to tests along the transverse direction.

205 With regard to the data from uniaxial tensile tests at disposal, the stretch along the loading

206 direction is experimentally evaluated. Considering that the first Piola-Kirchhoff stress tensor

207 depends on all the principal stretches and the stretch components that are not experimentally

208 evaluated must be calculated by analytical methods, as reported by the following equations:

$$209 \quad P_{ij}(\lambda_i, \lambda_j, \lambda_k) = 0, \quad P_{kk}(\lambda_i, \lambda_j, \lambda_k) = 0 \quad (17)$$

210 The subscript  $i$  specifies the loading direction depending on the specific experimental

211 situation, as apex-to-base or transverse directions. The stress components along the remaining

212 directions  $j$  and  $k$  are null, because of the uniaxial configuration of experimental tests.

213 Accounting for the experimental value of stretch component  $\lambda_i^{\text{exp}}$ , the solution of the

214 algebraic non-linear system, as reported in (17) leads to stretch components  $\lambda_j, \lambda_k$ , making it

215 possible to evaluate the nominal stress component  $P_{ii}(\lambda_i^{\text{exp}}, \lambda_j, \lambda_k)$  along the loading

216 directions.

217 The procedure adopted for the definition of the constitutive parameters requires the

218 minimization of the discrepancy between experimental and model results through a specific

219 cost function. The cost function used (Natali et al., 2010) is reported in equation (18) where

220 the weight of each data in the output is related with the ratio between the experimental data

221 and model results:

$$222 \quad \Omega(\boldsymbol{\omega}) = \sqrt{\frac{1}{n^1} \sum_{z=1}^{n^1} \left( 2 - \frac{P_{11}^{\text{exp}}}{P_{11}^{\text{mod}}(\boldsymbol{\omega}, \lambda_1^{\text{exp}})} - \frac{P_{11}^{\text{mod}}(\boldsymbol{\omega}, \lambda_1^{\text{exp}})}{P_{11}^{\text{exp}}} \right)} + \quad (18)$$

$$+ \sqrt{\frac{1}{n^2} \sum_{z=1}^{n^2} \left( 2 - \frac{P_{22}^{\text{exp}}}{P_{22}^{\text{mod}}(\boldsymbol{\omega}, \lambda_2^{\text{exp}})} - \frac{P_{22}^{\text{mod}}(\boldsymbol{\omega}, \lambda_2^{\text{exp}})}{P_{22}^{\text{exp}}} \right)}$$

223 where  $\boldsymbol{\omega}$  is the set of constitutive parameters,  $n^1$  and  $n^2$  the numbers of experimental data

224 along apex-to-base and transverse directions, respectively,  $\lambda_1^{\text{exp}}$  or  $\lambda_2^{\text{exp}}$  the  $z^{\text{th}}$

225 experimental input datum,  $P_{11}^{\text{exp}}{}_z$  or  $P_{22}^{\text{exp}}{}_z$  the  $z^{\text{th}}$  experimental output value, and  $P_{11}^{\text{mod}}{}_z$  or  
226  $P_{22}^{\text{mod}}{}_z$  the  $z^{\text{th}}$  model output result corresponding to the constitutive parameters  $\omega$  and the  
227 experimental input  $\lambda_1^{\text{exp}}{}_z$  or  $\lambda_2^{\text{exp}}{}_z$ . The function  $\Omega$  is a measure of the overall difference  
228 between experimental and model results when constitutive parameters  $\omega$  are adopted. The  
229 problem involves the evaluation of the set of constitutive parameters  $\omega_{\text{opt}}$  that minimizes  $\Omega$ .  
230

231 **RESULTS**

232 Results from experimental tests on tissue samples are reported in Figure 2. In detail average  
233 curves are reported for the different experimental situations investigated, as loading-  
234 unloading steps along different directions and according to different strain rates. Transverse  
235 specimens show a greater stiffness than apex-to-base ones. The result agrees with histological  
236 conformation of the tissue, as predominant distribution of muscular fibers along  
237 circumferential direction (Bouhout et al., 2013; Korossis et al., 2009; Zanetti et al., 2012). **The**  
238 **transverse response shows a greater influence of the strain rate on the stress-strain curve**  
239 **respect to the apex-to-base response, due to the different distribution of fibrous components**  
240 **along the different directions.** High level strain rates are adopted to outline the variation of  
241 tissue response in loading-unloading phases and to identify short term response more  
242 appropriately.

243 The analysis of data from experimental investigations allowed to provide a visco-hyperelastic  
244 constitutive formulation, whose parameters have been identified by the inverse analyses of  
245 the mechanical tests. The optimal parameters are reported in Tables 2 and 3, with regard to  
246 hyperelastic and viscous contributions, respectively. According to the histological  
247 conformation of the tissue and the results from experimental activities, hyperelastic  
248 parameters  $C_4, \alpha_4$  which characterize the fibers stiffness along apex-to-base direction, assume  
249 smaller values than  $C_6, \alpha_6$  which characterize the fibers stiffness along transverse direction.

250 The capability of the model to interpret the mechanical behavior of bladder tissues is reported  
251 in Figures 3 and 4. With regard to the different loading conditions investigated, experimental  
252 data, as average trends and scatter bands evaluated per sample, and model curves are  
253 compared in Fig. 3a-e and Fig. 4a-e. Model results are proposed again in Fig. 3f and Fig. 4f.  
254 Results from the loading steps only are reported, to better show the influence of strain rate on  
255 the mechanical response. **An additional analysis has been performed in order to check results**

256 affinity between the different pigs, demonstrating the marginal influence of the specific  
257 animal on variability of experimental data.

258 In order to further evaluate the capability of the model to interpret dissipative phenomena, the  
259 areas of hysteresis cycles are computed. Experimental and model results are compared in  
260 Figure 5.

261 Finally, the developed constitutive framework is applied to evaluate bladder tissue response  
262 under different loading conditions, as repetitive cyclic loading and stress relaxation. With  
263 regard to the former situation, model results for loading tests along apex-to-base and  
264 transverse directions are reported in Figure 6. The peak stress and the hysteresis area  
265 progressively decrease with the number of cycles up to stabilization.

266 **DISCUSSION AND CONCLUSION**

267 The constitutive analysis of bladder tissues is performed to provide a visco-hyperelastic  
268 framework that is capable to interpret the general features of bladder tissues mechanics. The  
269 analysis requires an integrated approach, accounting for the review of histological data to  
270 evaluate the tissues structural configuration, the design and development of experimental  
271 tests to provide the mechanical data, the constitutive model and to identify the associated  
272 parameters. The testing protocol included storing specimens at  $-20^{\circ}\text{C}$ , as done also by other  
273 authors (Dahms et al. 1998Tissue). As illustrated in the following, results agree with finding  
274 of other researchers who simply stored the biological material at  $+4^{\circ}\text{C}$  and tested it within 48  
275 h (Van Mastrigt et al., 1981; Salinas et al., 1992; Nagatomi et al., 2004). Nevertheless, a  
276 systematic analysis of the effects of storage temperature on mechanical properties of the  
277 specific tissue is still lacking in literature, while experience confirms the poor effects in other  
278 soft tissues.

279 Tissue conformation suggests to perform mechanical tests along different loading directions.  
280 Marginal discrepancies are found in literature data along the transverse direction compared to  
281 the apex-to-base direction, probably due to the strain levels assumed, where collagen fibres  
282 elongation becomes the dominant phenomenon (Korossis et al., 2009). The dissipative  
283 behavior does not show a high level of anisotropy, and this result is in accordance with  
284 observations from other authors (Regnier et al., 1983; Salinas et al., 1992; Nagatomi et al.,  
285 2004; Chen et al., 2013). Accounting for the histological data at disposal and results from the  
286 developed mechanical tests, a constitutive formulation is provided in the framework of fibre-  
287 reinforced composite materials visco-hyperelasticity. Considering the histological data  
288 reported in the literature (Bouhout et al., 2013; Korossis et a. 2009) and results from the  
289 developed mechanical tests, the constitutive parameters are identified by the inverse analysis  
290 of the experimental tests. The capability of the proposed constitutive formulation to interpret



291 the mechanics of bladder tissues is shown in Fig. 2, 3 and 4. From a qualitative point of view,  
292 model results well interpret the trends of the experimental data. From a quantitative point of  
293 view, model curves are well placed within the domains of the experimental results, and the  
294 calculated energy loss values fall within the variability of experimental data, and are  
295 generally very close to their average value. With specific regard to viscous phenomena, the  
296 identified parameters (Table 3) agree with results from other authors (Van Mastrigt et al.,  
297 1981; Salinas et al., 1992; Nagatomi et al., 2004).

298 The constitutive formulation also allowed to forecast tissue behaviour whenever the specimen  
299 undergoes consecutive cycles. According to both model and experimental results, the  
300 mechanical properties of the tissue change significantly. More likely, it shows that the  
301 employed loading rate in cyclic tests has not allowed full tissue recovery (Bischoff et al.,  
302 2004). Finally, according to the set up model, the stress relaxation behaviour is strongly  
303 dependent on strain rate: at lower strain rate, the tissue response is slower, reaching a smaller  
304 peak stress, and decaying with a longer time constant.

305 Analyses are developed to verify the capability of the constitutive model developed to  
306 interpret the mechanical response of the bladder tissue in physiological condition. Additional  
307 model results from stress relaxation conditions are reported in Figure 7. Stress relaxation  
308 phenomena are investigated assuming a 50% stretch condition which is reached according to  
309 different strain rates aiming at an interpretation of physiological condition.

310 Further investigations should be developed to improve the efficacy of results. Different  
311 loading conditions should be analyzed, as tensile tests along different directions to assess the  
312 assumption about anisotropic configuration and bi-axial tests to better evaluate the planar  
313 response. Nevertheless, the here proposed activities allows to quantitatively appreciate the  
314 typical features of bladder tissue mechanics, as direction dependence, non-linear elasticity  
315 and time-dependence. The experimental activities have been developed on animal model,

316 because of the availability of samples and the similarity between pig and human bladder  
317 structures. Aiming at the characterization of human bladder tissue mechanics, the further step  
318 of the investigation will have to account for the development of experimental activities on  
319 human samples. The number of samples will be necessarily small. The qualitative trend of  
320 tissue mechanics will be identified by the results from the experimental activities on pig  
321 samples, while the quantitative behavior will be tuned by the results from activities on human  
322 tissue.

323 The proposed constitutive analysis provides a procedure that should be adopted to perform  
324 the mechanical characterization of the different tissues of the urinary tract, which is  
325 mandatory for the definition of numerical models of the biological structures. In this way it is  
326 possible to investigate tissues response in healthy conditions and can be extended to  
327 degenerative conditions in the light of previous experience on damage models in soft tissue  
328 mechanics (Natali et al., 2003; Natali et al., 2008). Experience in surgical practice confirms  
329 the capability to provide a substitution following radical cystectomy (Abol-Enein et al., 2001;  
330 Kock et al., 1982; Hautmann et al., 1999; Pagano et al., 1990; Stein et al., 2004; Studer et al.,  
331 2006) by means of a specific technique that entails the use of substitute tissues that must  
332 guarantee the biomechanical performances, also in case of aged patients and considering  
333 potential local degenerative conditions. In fact, the present work must be considered as a  
334 preliminary step for the interpretation of biomechanical functionality and its correlation with  
335 surgical techniques. More in detail, the attention must be focused on mechanical actions  
336 induced on biological tissues during surgery and in the post-surgical configuration. It must be  
337 pointed out that computational methods allow the evaluation of structural data as the strain  
338 and stress fields, able to identify the tissue response. These data cannot be acquired by  
339 experimental techniques, with the same accuracy and richness of information, while they are  
340 mandatory for a reliable assessment of the applied mechanical actions.

341

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345

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347

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**1 FIGURE AND TABLE LEGENDS**

2 **Table 1.** Number of specimen and their average width and thickness.

3 **Table 2.** Set of hyperelastic constitutive parameters.

4 **Table 3.** Set of viscous constitutive parameters.

5 **Figure 1.** Bladder dissection and region definition: (a) bladder in the anterior-posterior view  
6 with indication of the track of dissection plane; (b) cut-opened bladder showing the apex, the  
7 lateral and the base region of the bladder.

8 **Figure 2.** Average experimental data along apex-to-base (AB) and transverse (T) direction:  
9 (a) strain rate 10 %/s, (b) strain rate 50 %/s, (c) strain rate 100 %/s, (d) strain rate 200 %/s, (e)  
10 strain rate 500 %/s.

11 **Figure 3.** Comparison of the tensile stress-strain along apex-to-base (AB) direction of  
12 experimental data (average  $\pm$  standard deviation) and analytical results: (a) strain rate 10 %/s,  
13 (b) strain rate 50 %/s, (c) strain rate 100 %/s, (d) strain rate 200 %/s, (e) strain rate 500 %/s.  
14 (f) Analytical results for the rising branch of loading cycles, at different strain rates.

15 **Figure 4.** Comparison of the tensile stress-strain along transverse (T) direction of  
16 experimental data (average  $\pm$  standard deviation) and analytical results: (a) strain rate 10 %/s,  
17 (b) strain rate 50 %/s, (c) strain rate 100 %/s, (d) strain rate 200 %/s, (e) strain rate 500 %/s.  
18 (f) Analytical results for the rising branch of loading cycles, at different strain rates.

19 **Figure 5.** Strain energy loss at different rates: comparison between experimental (average  $\pm$   
20 standard deviation) and analytical data, for (a) apex-to-base and (b) transverse directions.

21 **Figure 6.** Stress strain cycles, as predicted by the model, at strain rate 200%/s, for (a) apex-  
22 to-base and (b) transverse directions.

23 **Figure 7.** Stress relaxation curves predicted by the constitutive model, at different rates, for  
24 (a) apex-to-base and (b) transverse directions.

25



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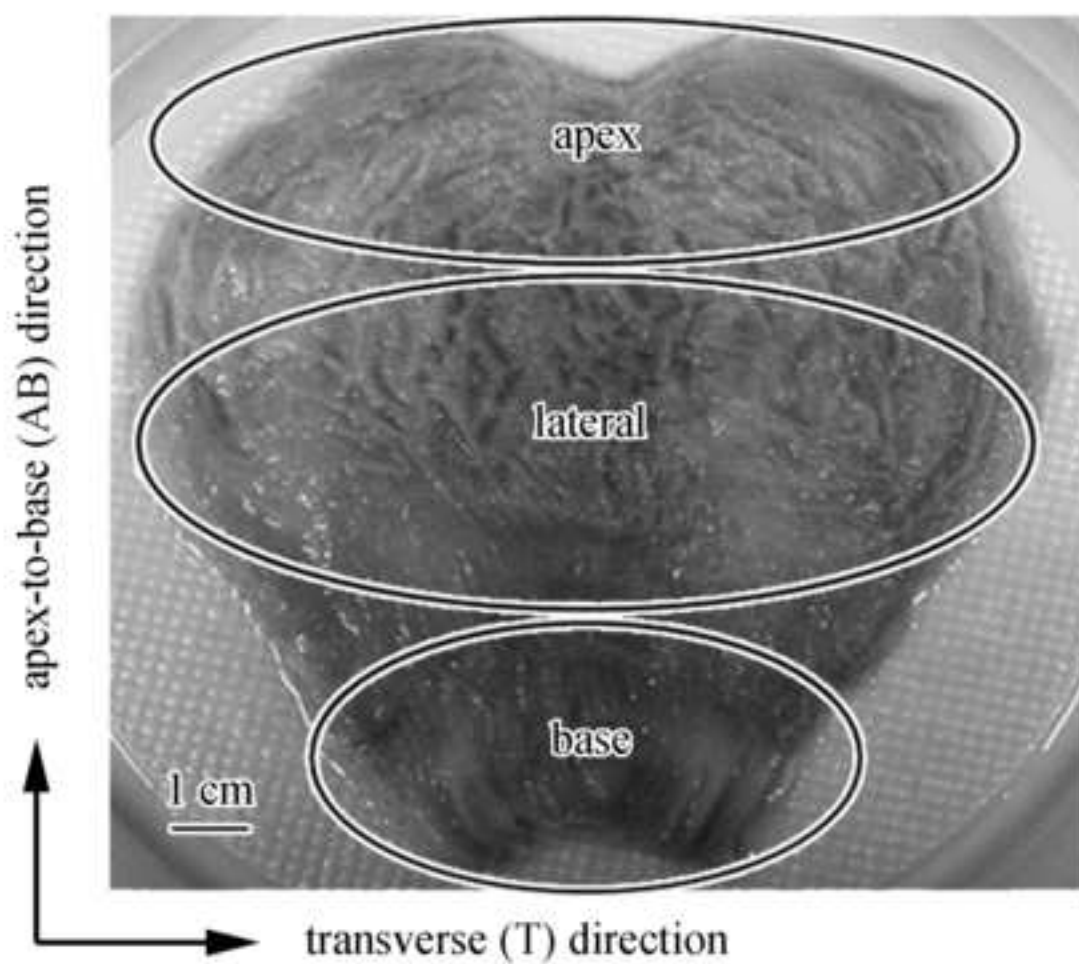
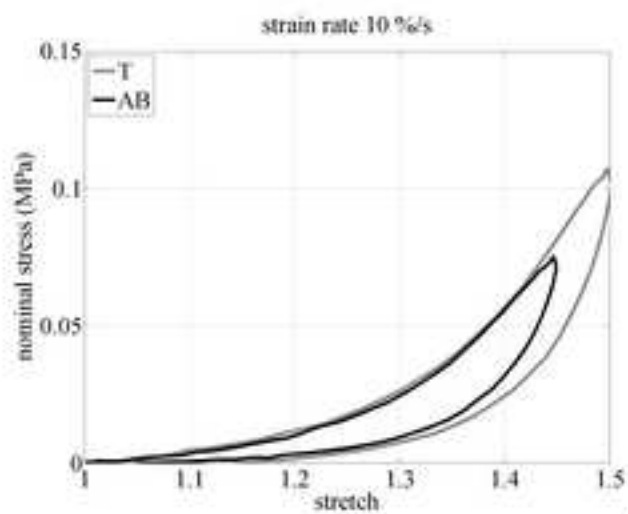
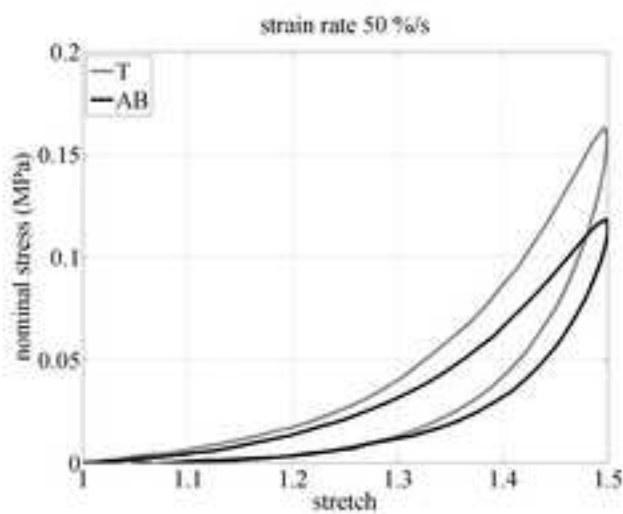


Figure 2

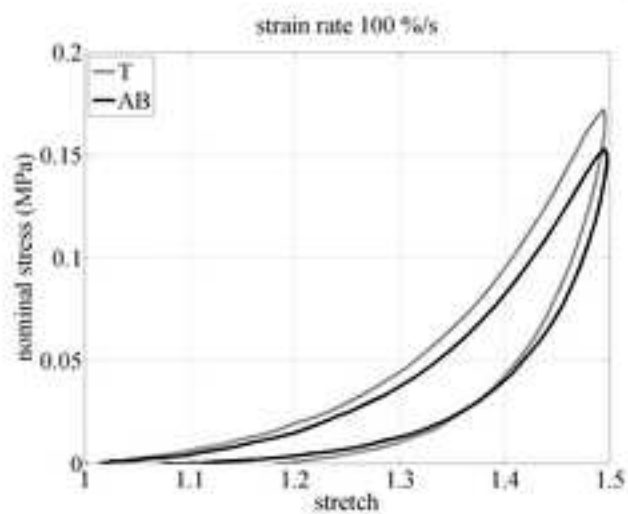
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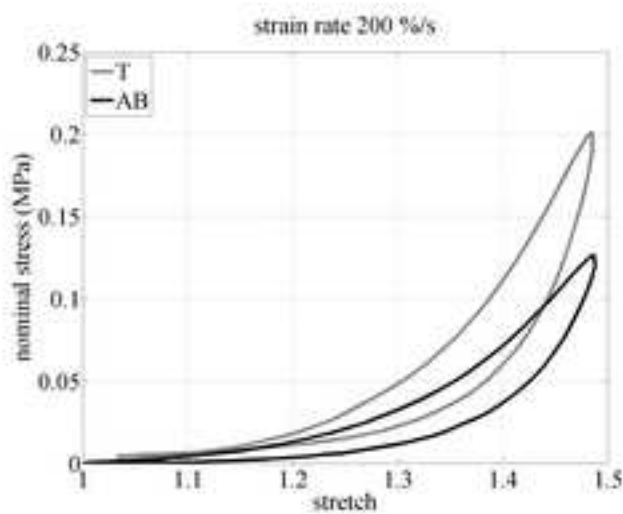
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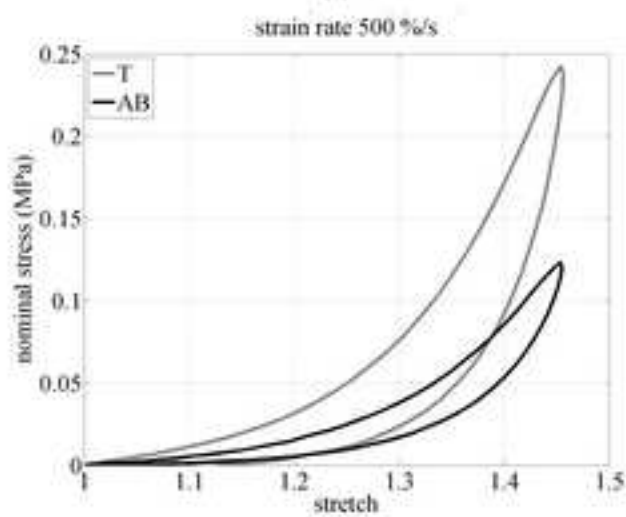
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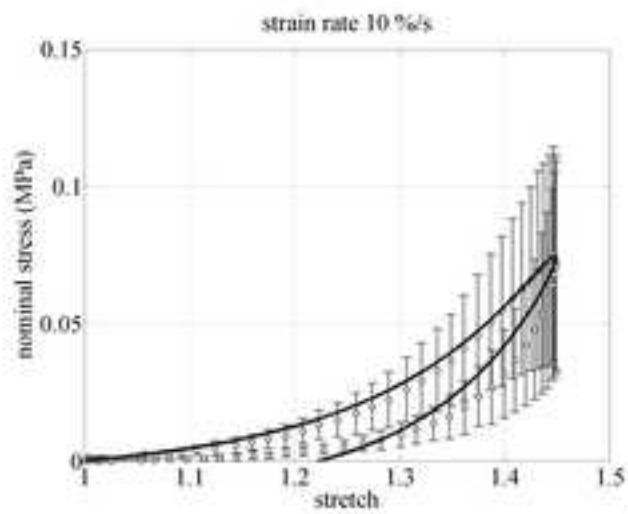


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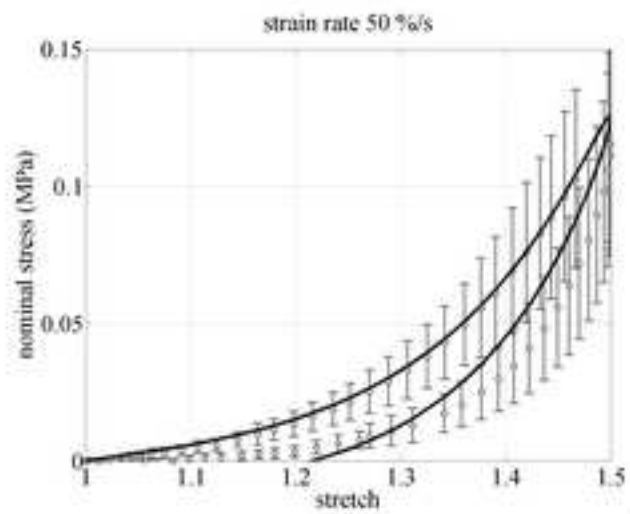


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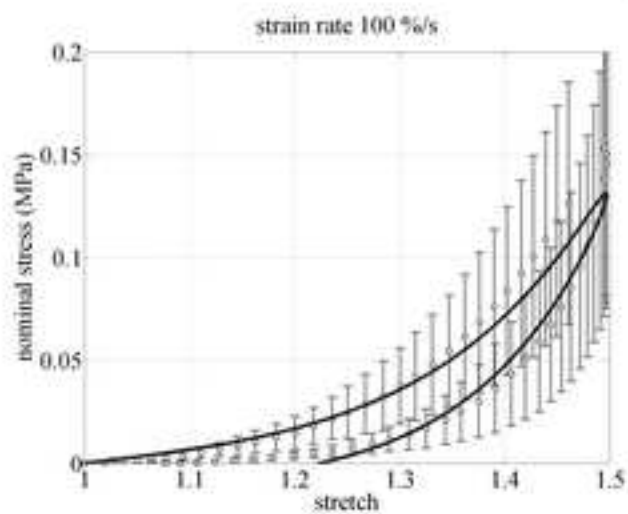
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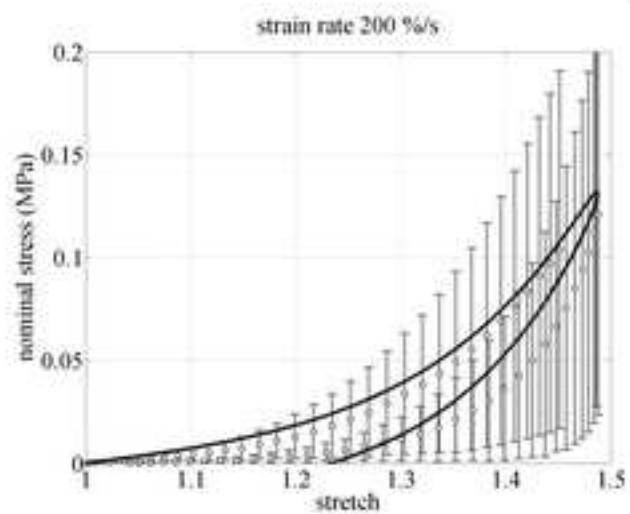
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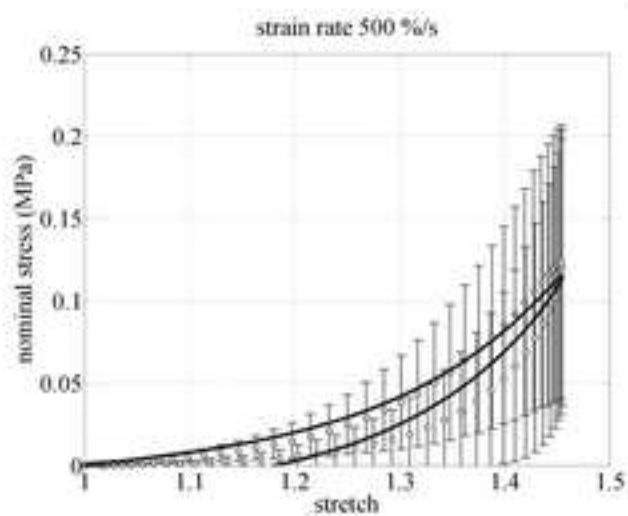
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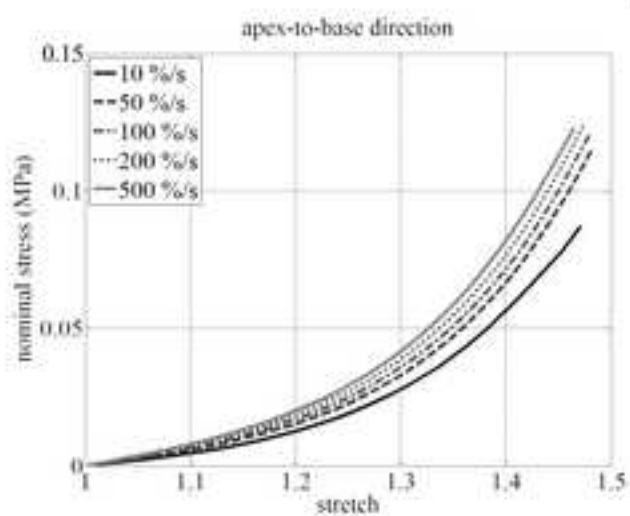
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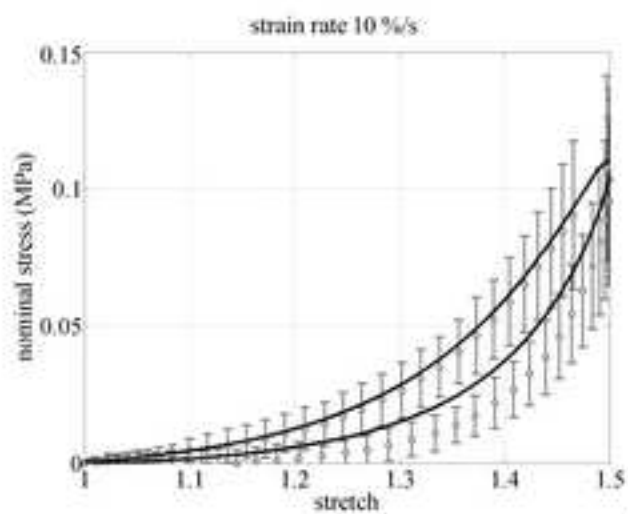
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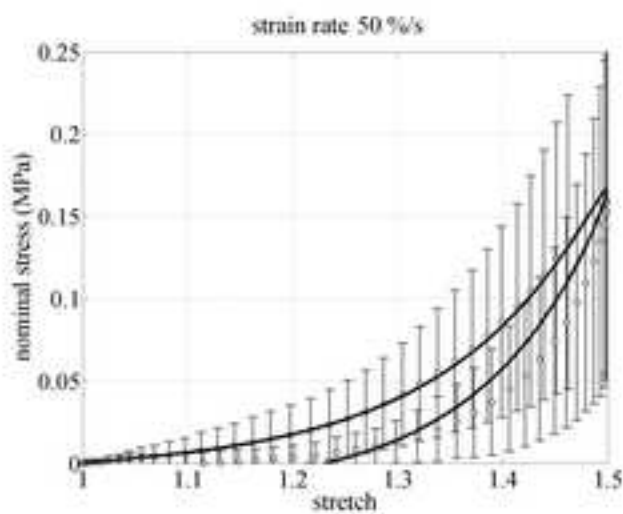
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Figure 4

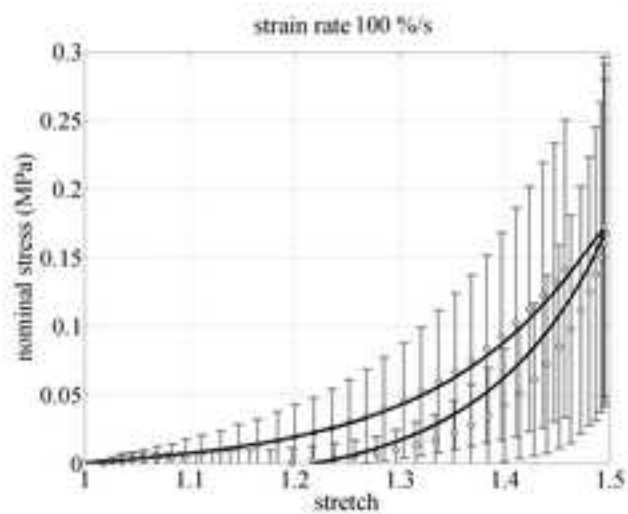
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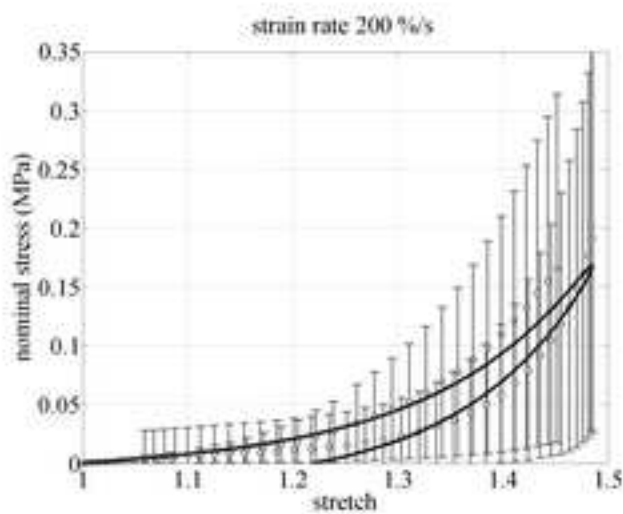
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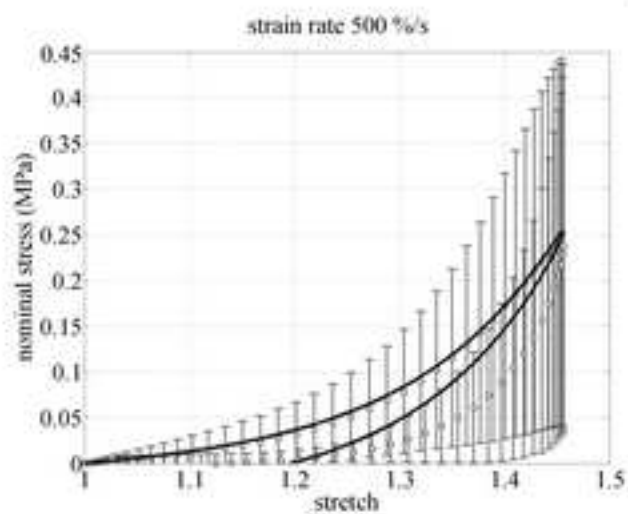
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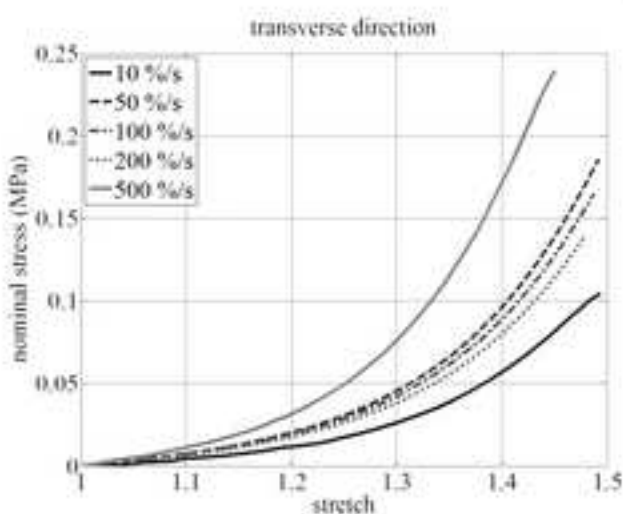
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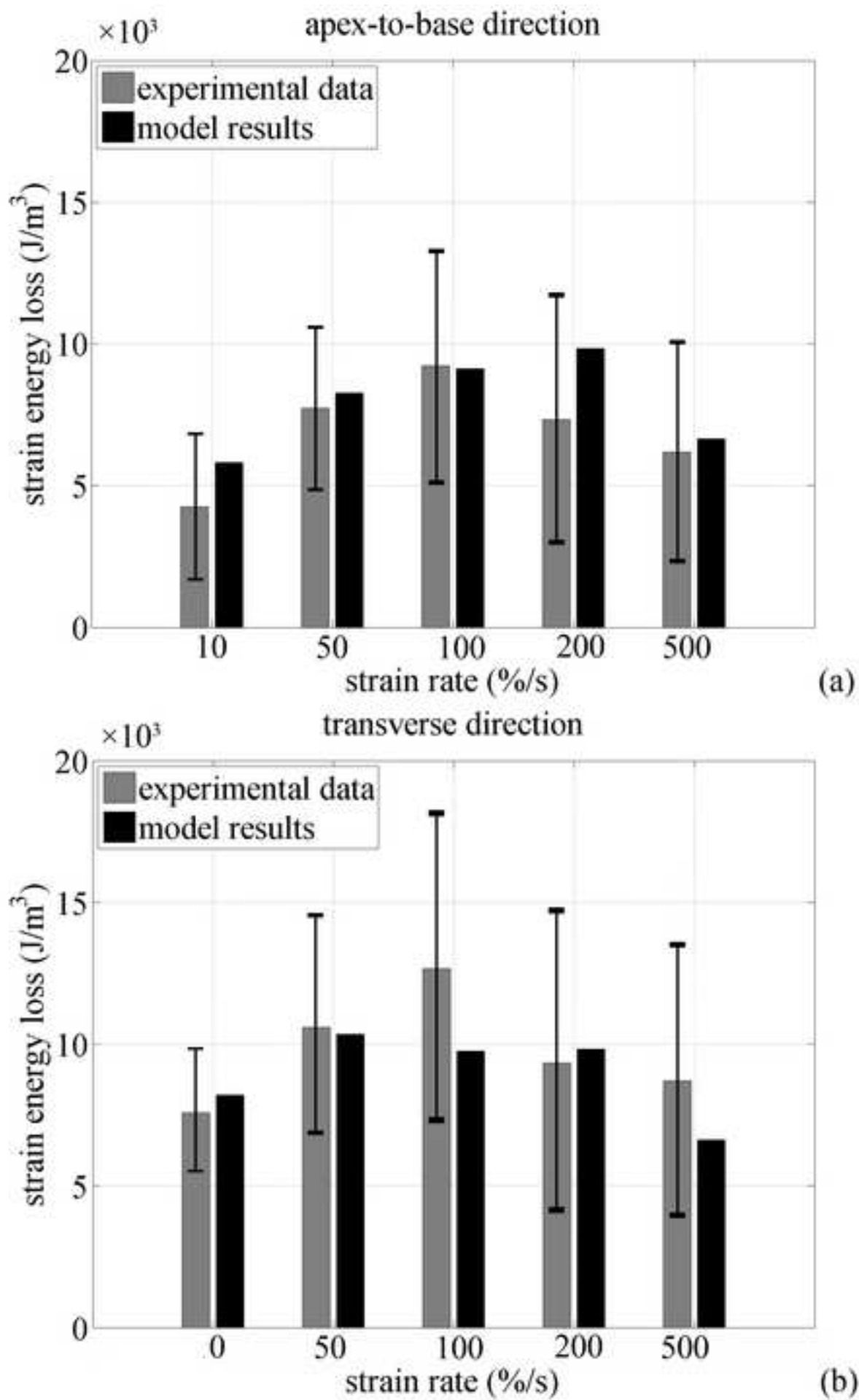


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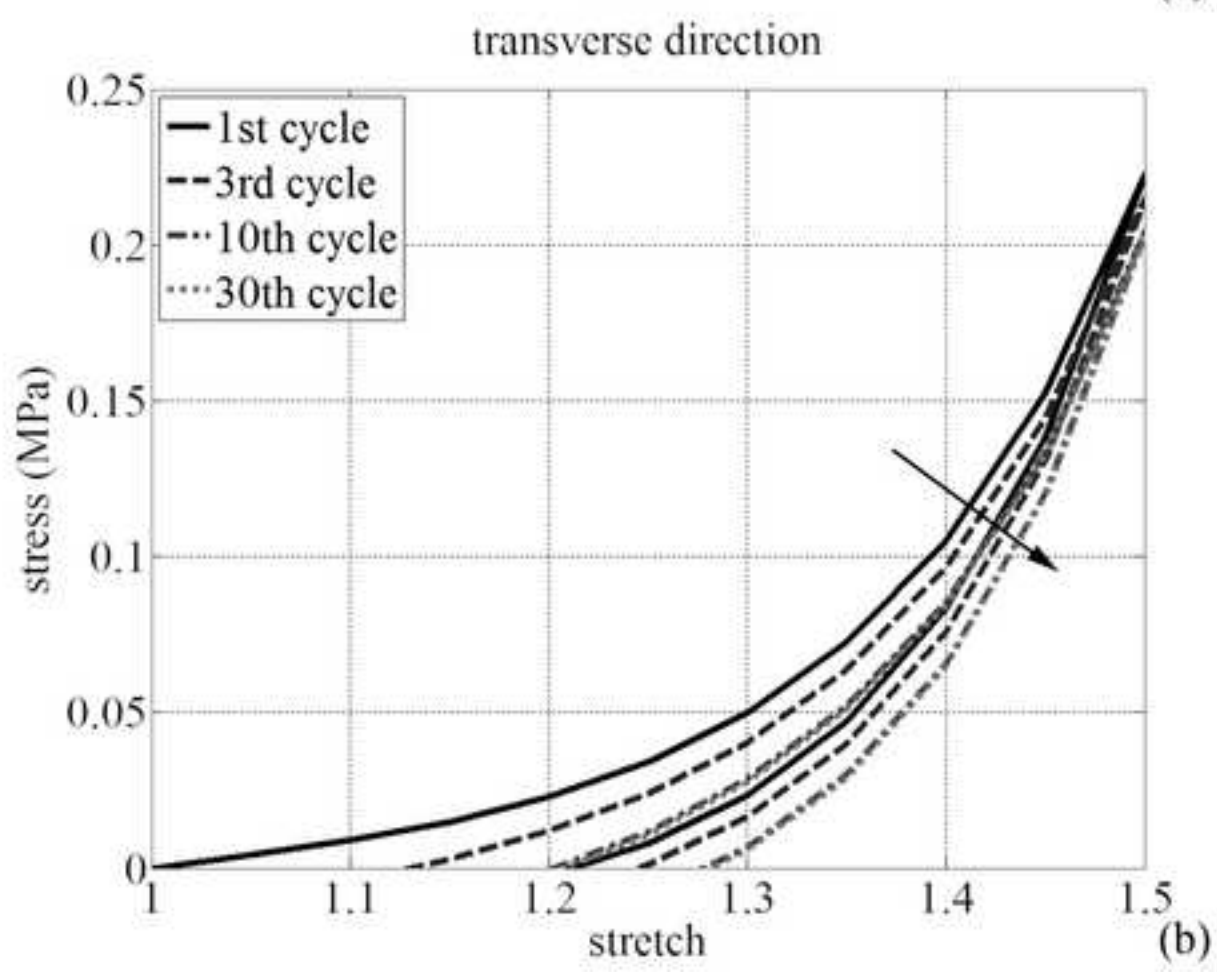
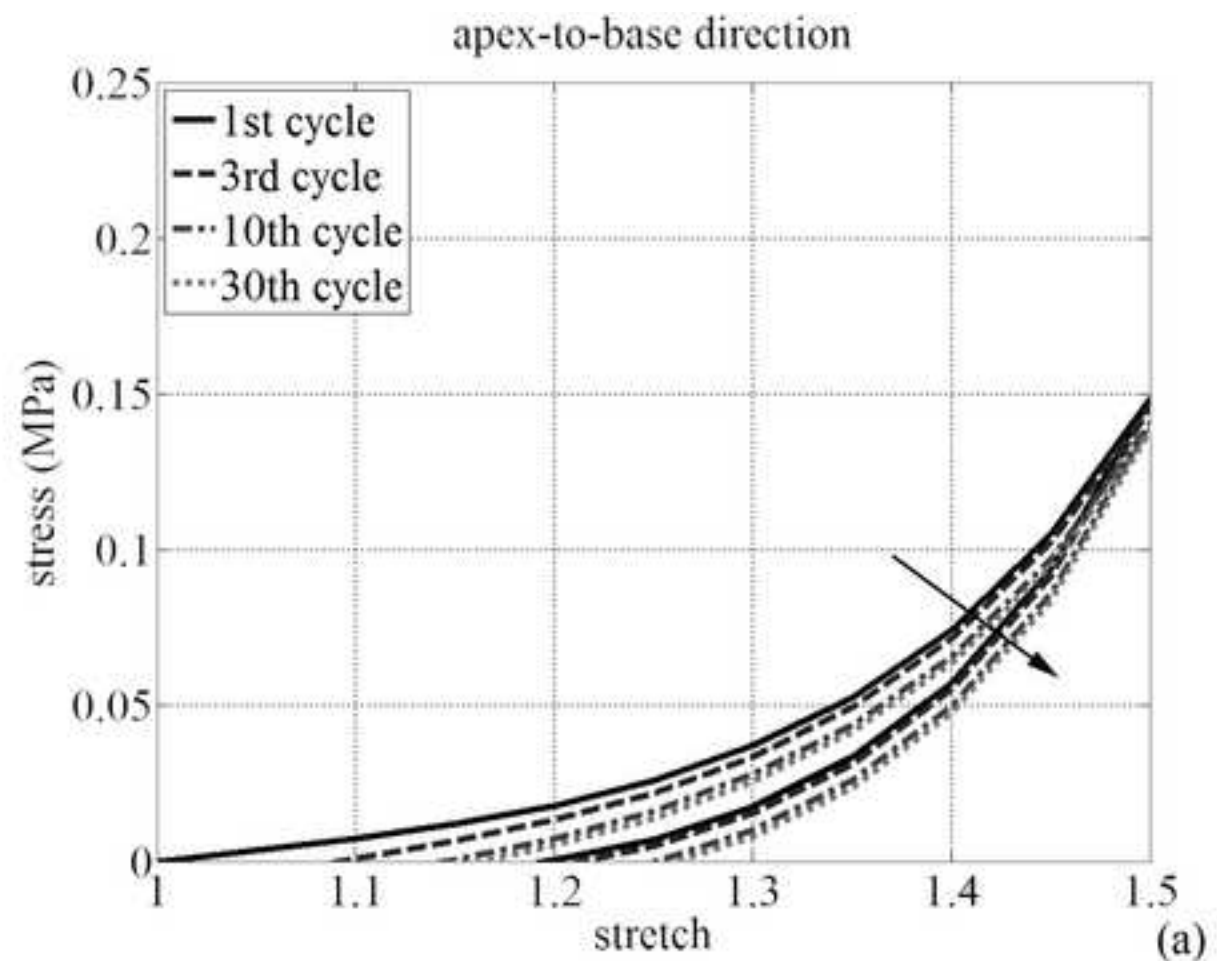
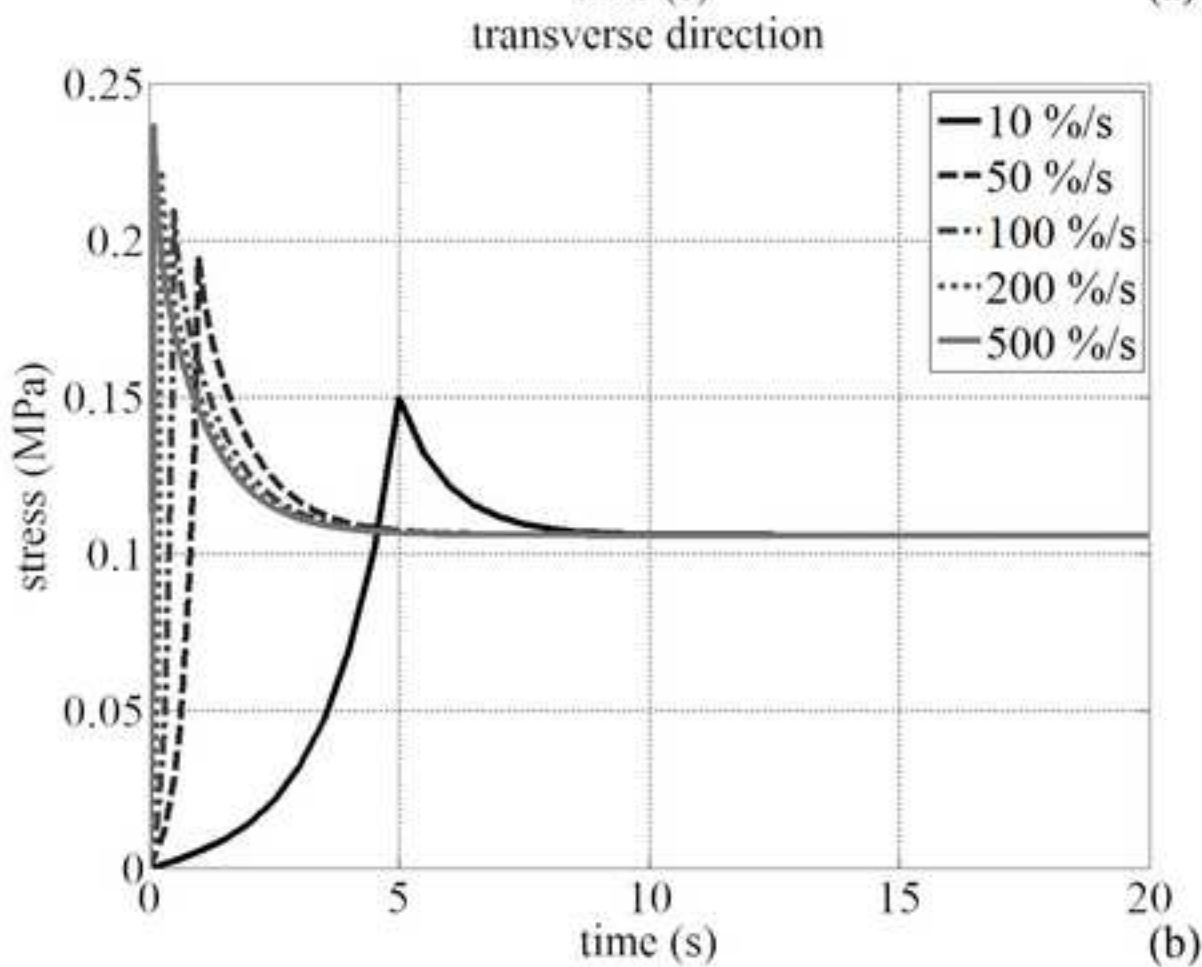
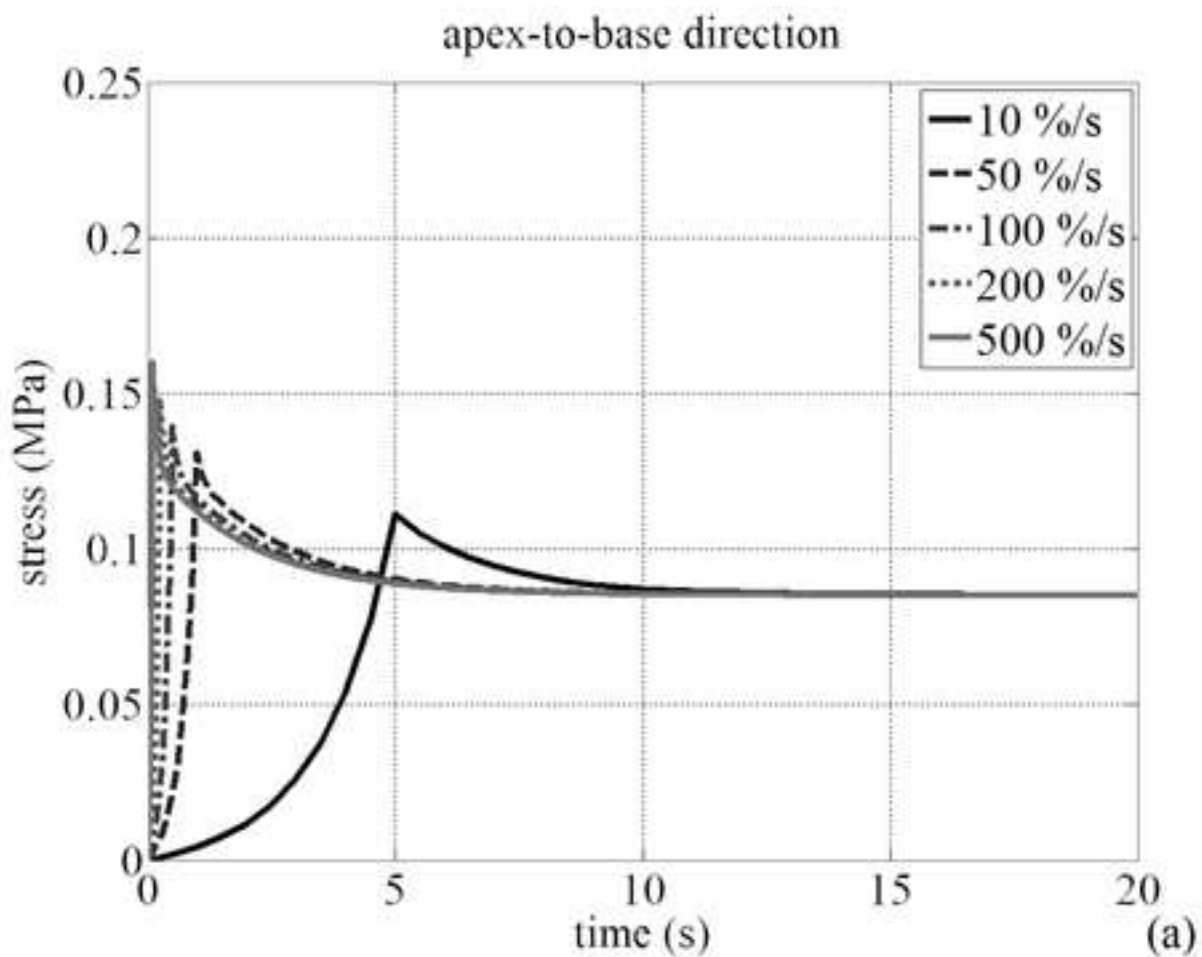


Figure 7

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## TABLES

	No. of specimen	width mean $\pm$ standard deviation (mm)	thickness mean $\pm$ standard deviation (mm)
apex-to-base direction	9	4.95 $\pm$ 0.56	4.37 $\pm$ 1.00
transverse direction	16	4.49 $\pm$ 0.78	3.77 $\pm$ 1.03

Table 1

$C_1$ (MPa)	$\alpha_1$	$C_4$ (MPa)	$\alpha_4$	$C_6$ (MPa)	$\alpha_6$
$5.96 \cdot 10^{-4}$	$2.20 \cdot 10^0$	$4.60 \cdot 10^{-3}$	$2.04 \cdot 10^0$	$4.80 \cdot 10^{-3}$	$2.25 \cdot 10^0$

Table 2

	$\gamma$	$\tau$ (s)
matrix viscous process ( $m$ )	$9.37 \cdot 10^{-1}$	$8.50 \cdot 10^{-2}$
apex-to-base viscous process ( $fAB$ )	$3.50 \cdot 10^{-1}$	$2.32 \cdot 10^{+0}$
transversal viscous process ( $fT$ )	$4.12 \cdot 10^{-1}$	$2.01 \cdot 10^{+0}$

Table 3