

Environmental effects on natural frequencies of the San Pietro bell tower in Perugia, Italy, and their removal for structural performance assessment

Filippo Ubertini^{a,d}, Gabriele Comanducci^a, Nicola Cavalagli^a, Anna Laura Pisello^{b,c}, Annibale Luigi Materazzi^a, Franco Cotana^b

^a*Department of Civil and Environmental Engineering, University of Perugia, Via G. Duranti 93, 06125 Perugia, Italy*

^b*CIRIAF Interuniversity Research Center on Pollution and Environment “M. Felli”, University of Perugia, Via G. Duranti, 06125 Perugia, Italy*

^c*Department of Engineering, University of Perugia, Via G. Duranti 1/A4, 06125 Perugia, Italy*

^d*Corresponding author, phone: +39 075 585 3954; fax: +39 075 585 3897; e-mail: filippo.ubertini@unipg.it*

Abstract

Continuously identified natural frequencies of vibration can provide unique information for low-cost automated condition assessment of civil constructions and infrastructures. However, the effects of changes in environmental parameters, such as temperature and humidity, need to be effectively investigated and accurately removed from identified frequency data for an effective performance assessment. This task is particularly challenging in the case of historical constructions, that are typically massive and heterogeneous masonry structures characterized by complex variations of materials’ properties with varying environmental parameters and by a differential heat conduction process where thermal capacity plays a major role.

While there is abundance of documented monitoring data highlighting correlations between environmental parameters and natural frequencies in the case of new structures, such as long-span bridges, similar studies for historical constructions are still missing, with only a few literature works occasionally reporting increments in natural frequencies with increasing temperature of construction materials due to the closure of internal micro-cracks in the mortar layers caused by thermal expansion.

In order to gain some knowledge on the effects of changes in temperature and humidity on the natural frequencies of slender masonry buildings, the

paper focuses on the case study of an Italian monumental bell tower that has been monitored by the authors for more than nine months. Correlations between natural frequencies and environmental parameters are investigated in details and the predictive capabilities of linear statistical regressive models based on the use of several environmental continuous monitoring sensors are assessed. At the end, three basic mechanisms governing environmentally-induced changes in the dynamic behavior of the tower are identified and essential information is achieved on the optimal location and minimum number of environmental sensors that are necessary in a structural health monitoring perspective.

Keywords: structural health monitoring, environmental effects, cultural heritage preservation, historical constructions, weather conditions, continuous hygro-thermal monitoring, operational modal analysis.

1. Introduction

Extracting dynamic signatures from vibrating structures and inspecting their variations is becoming a popular engineering practice for automated structural performance assessment and early stage damage detection [1], whereby a structural damage can be in many cases detected as a modification in the global dynamic behavior of the structure [2, 3]. This automated detection of small changes in structural performance, typically produced by earthquakes or by other types of dynamic loadings, allows a cost-effective management of maintenance and restoration interventions which is named condition-based maintenance as opposite to breakdown-based or periodic maintenance [4].

While traditionally applied to civil infrastructure [5], vibration-based structural health monitoring (SHM) techniques appear to be very promising for applications to slender historical and monumental structures, such as civic towers and bell towers [6]. This is due to their fully non-destructive character and the relatively inexpensive equipment that is necessary for testing (usually a small number of high sensitivity accelerometers and off-the-shelf devices for data acquisition, storage and analysis), resulting in historical and architectural respect conforming to international criteria and protocols on cultural heritage preservation. Despite all these advantages, only a few applications of continuous vibration-based SHM systems to cultural heritage constructions have been documented so far [7], whereby the majority of the authors

23 have limited their attention to ambient vibration testing for complementing
24 vulnerability assessment through calibration of finite element models: the
25 interested reader could benefit of literature devoted to applications to histor-
26 ical bridges [8, 9, 10], monumental buildings [11, 12, 13, 6, 14] and historical
27 towers [15, 16, 17, 18, 19, 20, 21]. A more widespread application of contin-
28 uous SHM in the context of historical constructions is however expected in
29 the near future, especially as it concerns civic and bell towers that typically
30 exhibit higher amplitudes of vibration in comparison to low-rise buildings,
31 thus being comparatively more suited for dynamic monitoring.

32 Natural frequencies of vibration have recently been rediscovered as very
33 effective and convenient damage sensitive features for vibration-based SHM
34 [22]. One main reason making natural frequencies so attractive is that reliable
35 automated operational modal analysis (OMA) techniques have been devel-
36 oped in recent years [23, 24, 25], allowing an accurate estimation of natural
37 frequencies from in-service response data, typically using a small number of
38 off-the-shelf sensors and without requiring any manual intervention. Unfortu-
39 nately, natural frequencies have the main drawback of being strongly affected
40 by environmental conditions and above all key weather parameters, such as
41 temperature and humidity [1] as well as, in the case of very slender struc-
42 tures, wind speed [26]. In order to cope with this issue, some authors have
43 proposed to remove the part of variance in the data associated with changing
44 environmental conditions through the use of proper statistical models, such
45 as multiple data regressions [27] and principal component analysis (PCA)
46 [28, 29, 30] and to detect anomalies in the structural behavior by means of
47 statistical process control tools such as control charts [27, 31, 32]. While
48 the mechanisms governing environmentally-induced variations of natural fre-
49 quencies in modern structures have been mostly clarified, characterization
50 and removal of the key environmental effects from continuously identified
51 natural frequencies of historical masonry constructions is still an open prob-
52 lem, due to the lack of documented permanent monitoring campaigns in
53 such kind of structures. In this context, some authors reported an increase
54 in the natural frequencies of vibration of global modes of masonry towers
55 with increasing outdoor dry bulb temperature due to thermal expansion in
56 the masonry determining closing of micro-cracks in mortar layers [6, 7], but
57 the knowledge in this field needs further investigation as addressed in this
58 research work.

59 This paper presents an in-depth characterization of environmental ef-
60 fects on the natural frequencies of vibration of a monumental masonry bell

61 tower, the San Pietro bell tower in Perugia, Italy, where the authors have
62 recently installed a permanent vibration-based SHM system. The paper is or-
63 ganized as follows. Section 2 presents the case study historical tower and the
64 multipurpose monitoring system. Section 3 investigates correlations among
65 environmental parameters and among natural frequencies, as well as cross-
66 correlations between natural frequencies and the monitored environmental
67 parameters. Section 4 addresses the task of statistical estimation of natural
68 frequencies from independent environmental measurements by investigating,
69 in particular, the role played by the number of environmental monitoring
70 sensors, their optimal placement and the length of the training period nec-
71 essary for identifying the statistical models. Finally, Section 5 concludes the
72 paper.

73 **2. Continuous structural health monitoring of a monumental ma-** 74 **sonry bell tower**

75 *2.1. The bell tower*

76 The case study considered in this paper is the bell tower of the Benedictine
77 Abbey of San Pietro in Perugia, Italy, Figure 1. This monumental masonry
78 tower, erected for the first time in the 13th century, can be considered as
79 one of the major monuments of the City, owing to its unique architectural
80 character and to its location on top of a hill from where it dominates the
81 civic skyline.

82 With its total height of 61.45 m, the tower can be roughly subdivided
83 in four main parts. The lowest section, termed basement, has a cone shape
84 and reaches the height of about 8 m. The portion of the tower erected over
85 the basement and reaching the height of 26 m is termed shaft and has a
86 dodecagonal cross section. Both basement and shaft are made of hollow
87 masonry with an internal core made of heterogeneous material. The total
88 width of the walls of the basement ranges from 3.2 m on the base to about 2 m
89 on the top. The external surfaces of such walls are made of regular calcareous
90 stone blocks with some brick local replacements, while internal surfaces are
91 made of less regular stone masonry. The four bells are located in the belfry
92 that has an hexagonal cross-section and reaches the height of 41 m. The
93 belfry is architecturally characterized by large Gothic openings presenting
94 external frames and columns made of a mixed travertine-calcareous stone
95 masonry with some brick replacements. The internal surface of the belfry
96 is instead entirely made of brick masonry. Above the belfry, the tower is

97 completed by the cusp that has the shape of a pyramid with hexagonal cross-
98 section and is made of a mixed travertine-calcareous stone masonry with an
99 external cover in brick masonry.

100 The bell tower as it appears today is the result of various structural
101 and architectural modifications occurred through the centuries. The most
102 invasive intervention was made in the 14th century when the tower was fully
103 demolished and rebuilt as a defensive building. The final design, in Florentine
104 Gothic style, was probably developed by Bernardo Rossellino in the 15th
105 century. Other, more limited modifications to the structure showed to be
106 necessary in order to repair damages caused by lightnings. In 1932, the
107 vault at the base of the belfry was partially demolished in order to install
108 the metallic structure that still supports the four bells. This intervention
109 was probably motivated by the necessity to better distribute the dynamic
110 loads that the swinging bells exerted on the structure. In 2002, the tower
111 was repaired in order to fix the damages caused by the strong earthquake
112 that occurred in Umbria and Marche central Italian regions in 1997. This
113 intervention mostly affected the belfry and the cusp where damages were
114 concentrated and consisted of grout injections at the base of the columns of
115 the belfry, installation of fiber rings on the cusp, to withstand the lateral
116 thrust at the top of the belfry, and application of longitudinal fiber strings
117 along the inner parts of the columns to prevent bending deformations [33].

118 Fig. 1 reports a photo evidence of the tower and a solid CAD model of
119 the structure highlighting its main geometrical characteristics.

120 *2.2. Monitoring hardware*

121 With the purpose of monitoring the structural integrity of the bell tower
122 and of promptly detecting damages caused by low-return period earthquakes,
123 a vibration-based SHM system has been installed by the authors at the end
124 of 2014. The system comprises three high sensitivity accelerometers perma-
125 nently installed at the base of the cusp and various environmental monitoring
126 sensors and proper data acquisition hardware. Monitoring data are locally
127 recorded and sent, through the Internet, to the Laboratory of Structural
128 Dynamics of University of Perugia, where they are processed in a dedicated
129 server for the purpose of modal tracking and SHM using a MatLab code [34]
130 developed by the authors for the purpose, and to the laboratories of CIRIAF
131 Interuniversity Research Centre on Pollution and Environment "Mauro Felli"
132 for the purpose of monitoring of weather and other environmental conditions.

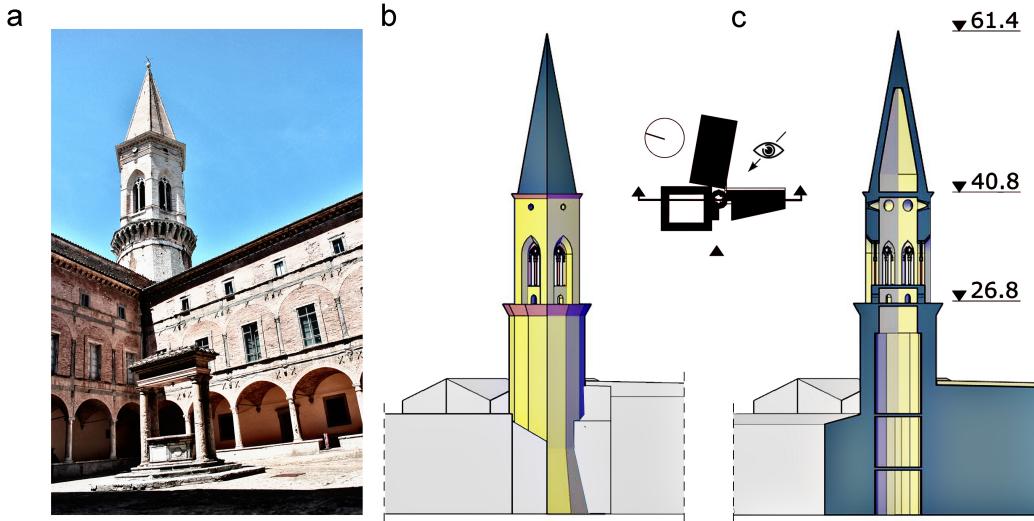


Figure 1: The bell tower of the Basilica of San Pietro (dimensions in m): photography from inner cloister (a); front view (b) and sectional view (c) from solid CAD model.

133 Accelerometers installed on site are uni-axial sensors model PCB 393B12
 134 with 10 V/g sensitivity. The sensors' layout, shown in Figure 2, allows to
 135 observe bending modes in the two orthogonal directions denoted as x and y ,
 136 as well as torsional modes.

137 With the purpose of achieving a spatially dense representation of the en-
 138 vironmental conditions of the tower, eight temperature sensors (six dry bulb
 139 temperature sensors and two surface temperature sensors) and two humid-
 140 ity sensors have been installed since March 2015 with the layout shown in
 141 Figure 2. In this way, SHM and environmental monitoring are combined,
 142 which stimulates the development of integrated structural-thermal-energy
 143 monitoring systems for historic buildings. Environmental sensors are Tiny-
 144 tag from Gemini Data Loggers, typically used in building physics applications
 145 [35, 36, 37] and representing robust environmental monitoring solutions for
 146 field application in difficult accessibility locations such as the case study of
 147 this work. Table 1 summarizes the main information about temperature mea-
 148 surements, numbered from T_1 to T_8 , and humidity measurements, denoted
 149 as ϕ_1 and ϕ_2 .

150 Data from accelerometers are acquired through a multi-channel system,
 151 carrier model cDAQ-9188 with NI 9234 data acquisition modules (24-bit res-

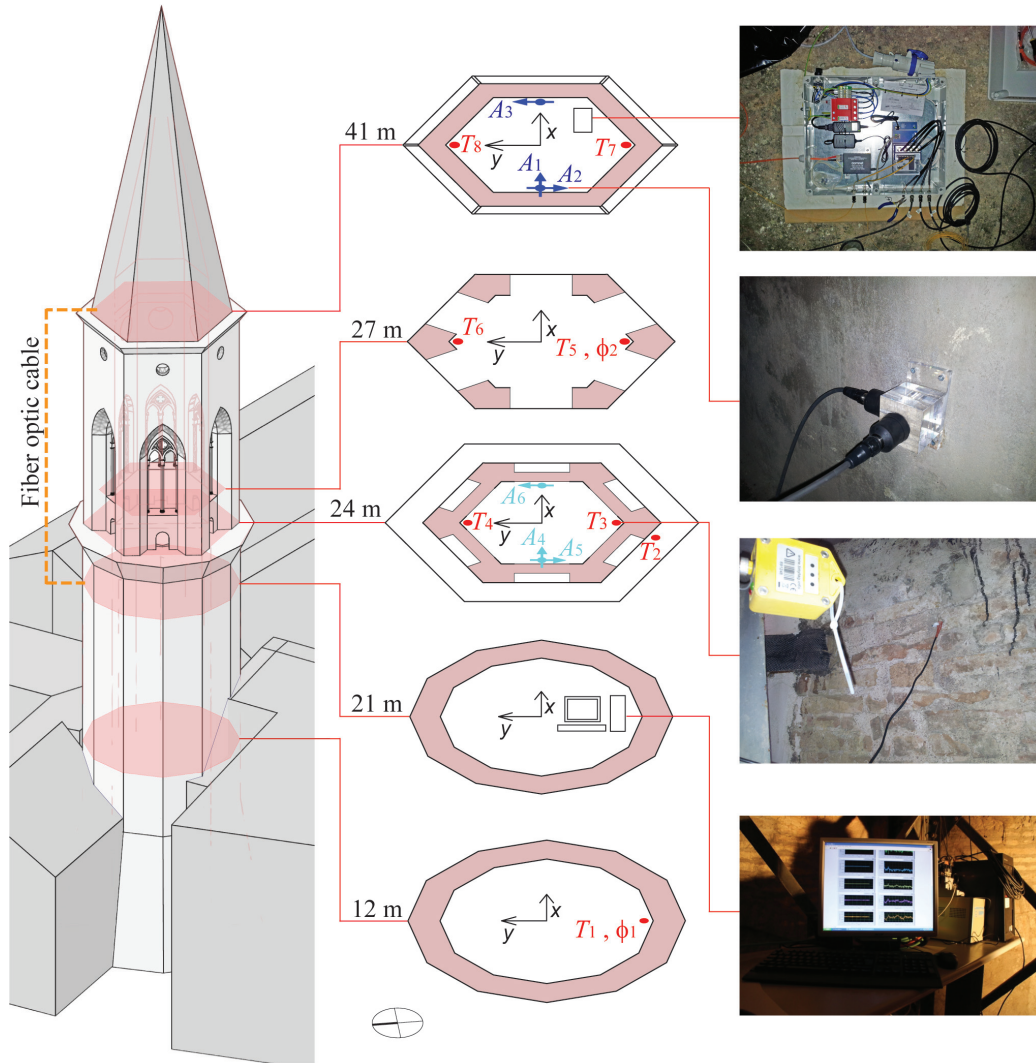


Figure 2: Sketch of the monitoring system with sensors positions and photo evidence of sensors on site and of data acquisition hardware (A , T and ϕ denote acceleration, temperature and humidity sensors, respectively). Acceleration sensors A_1 , A_2 and A_3 are used for permanent monitoring purposes, while sensors A_4 , A_5 and A_6 are only used in AVT.

152 olution, 102 dB dynamic range and anti-aliasing filters). Data from environ-
 153 mental sensors are acquired every 30 minutes and contemporary registered
 154 within independent dataloggers connected to each sensor.

Sensor no.	Variable name	Measurement type	Location	Height	Orientation
1	T_1	Air temperature	Shaft indoor	12 m	S
2	T_2	Surface temperature	Shaft outdoor	24 m	S
3	T_3	Surface temperature	Shaft indoor	24 m	S
4	T_4	Air temperature	Shaft indoor	24 m	N
5	T_5	Air temperature	Belfry outdoor	27 m	S
6	T_6	Air temperature	Belfry outdoor	27 m	N
7	T_7	Air temperature	Cusp indoor	41 m	S
8	T_8	Air temperature	Cusp indoor	41 m	N
9	ϕ_1	Air humidity	Shaft indoor	12 m	S
10	ϕ_2	Air humidity	Belfry outdoor	27 m	S

Table 1: Environmental monitoring sensors installed on the bell tower.

155 After the first months of monitoring, the system showed to be prone
 156 to overvoltage from the power line and to currents induced in wired con-
 157 nections by lightnings that quite often hit the tower during the year. In
 158 order to avoid consequent damaging to the monitoring hardware, the system
 159 has been occasionally shut down between December 2014 and August 2015,
 160 while protective countermeasures have been undertaken since August 2015.
 161 In order to avoid induced currents, accelerometers are connected to the data
 162 acquisition system using short cables, deployed in horizontal directions, or-
 163 thogonal to the direction of the lightning rods. The use of short cables also
 164 reduces noise in the signals. The data acquisition system is located at the
 165 base of the cusp and placed within a box that contains a protective system
 166 against overvoltage. Electrical disconnection between sensors and masonry
 167 is also achieved by screwing the accelerometers to Plexiglas blocks rigidly
 168 connected to the structure (see Figure 2). A dedicated computer is placed in
 169 an accessible location below the belfry and it is used for data storage and for
 170 data transmission through the Internet. This computer is connected to the
 171 data acquisition system located inside the cusp using a 30 m long vertical
 172 fiber optic network cable that does not transmit induced currents. The moni-
 173 toring system, including the protective system against lightnings, is depicted
 174 in Figure 2.

175 2.3. Continuous modal identification technique

176 Damage detection of the bell tower is based on the continuous identi-
 177 fication of its natural frequencies and on the inspection of their variations
 178 associated with local changes in stiffness. Vibration data are recorded at

179 1600 Hz, down-sampled to 40 Hz and stored in separate files of 30 recording
180 minutes for the purpose of modal identification.

181 Output only modal identification is carried out using 30-minutes long time
182 history acceleration data by means of a fully automated data-driven Stochastic
183 Subspace Identification (SSI-data) technique developed by the authors in
184 a previous study [25]. It is worth noting that the duration of the signals
185 contained in each monitoring file is fairly longer than what is classically sug-
186 gested in the literature (e.g. [38]) for an accurate modal identification, that
187 is, a duration larger than about 1000-2000 times the fundamental structural
188 period.

189 SSI-data establishes a mathematical model of the monitored structure,
190 based on output-only information, in the form of a linear-time-invariant sys-
191 tem under unknown excitation:

$$\begin{aligned} \mathbf{x}(k+1) &= \mathbf{A}\mathbf{x}(k) + \mathbf{w}(k) \\ \mathbf{y}(k) &= \mathbf{C}\mathbf{x}(k) + \mathbf{v}(k) \end{aligned} \quad (1)$$

192 where k is the generic time step and $\mathbf{x} \in \mathbb{R}^n$ is the state vector, n being the
193 order of the identified model. In eq. (1), $\mathbf{A} \in \mathbb{R}^{n \times n}$ is the system matrix from
194 which modal information is retrieved, $\mathbf{w} \in \mathbb{R}^n$ is the unknown external input,
195 modeled as a white noise vector process, $\mathbf{y} \in \mathbb{R}^l$ is the vector containing the
196 l output measurements, $\mathbf{C} \in \mathbb{R}^{l \times n}$ is the corresponding output matrix and
197 $\mathbf{v} \in \mathbb{R}^l$ is a white noise vector process representing the noise content of
198 the measurements. For the details on the theory of SSI-data, the interested
199 reader is referred to Ref. [39].

200 In the adopted automated identification procedure, the data-driven SSI
201 canonical variate analysis is performed for different values of the order of
202 the model in Eq. (1) and of the number of output block rows adopted to
203 construct the block Hankel matrix of the data [39]. Then, spurious noise
204 modes are eliminated on the basis of similarity checks between estimated
205 modal parameters and clustering of remaining modes is carried out. Finally,
206 mean values of modal parameters estimates with 95% confidence intervals
207 are extracted from each cluster of modes.

208 In the present application, the order of the model is varied from 40 to
209 60 with step increments of 2 and the number of output block rows is varied
210 from 140 to 200 with step increments of 10. Relative tolerances used for noise
211 modes elimination are: 0.01 for frequencies, 0.03 for modal damping ratios
212 and 0.01 for modal assurance criterion. Finally, a relative tolerance of 0.03
213 is used for clustering analysis as threshold in a similarity check comprising

214 both frequencies and eigenvectors. The interested reader is referred to Ref.
 215 [25] for specific details on the identification procedure.

216 2.4. Environmental effects removal and health assessment methodology

217 Environmental effects can be removed from identified natural frequency
 218 data using statistical techniques [27, 28, 29, 30]. In this paper, multiple linear
 219 regressive (MLR) filters are adopted for this purpose, where linear correla-
 220 tions between a set of r dependent variables (natural frequencies) and a set
 221 of p independent variables (environmental parameters), called predictors, are
 222 exploited. In the present case, modal frequencies are stored in an observation
 223 matrix, \mathbf{Y} , and an estimate, $\hat{\mathbf{Y}}$, of such a matrix is obtained as

$$\hat{\mathbf{Y}} = \boldsymbol{\beta}^T \mathbf{Z}^T \quad (2)$$

224 where matrix $\mathbf{Z} \in \mathbb{R}^{N \times p+1}$ contains a first column of ones and p columns
 225 containing N values of the p selected environmental parameters, while matrix
 226 $\boldsymbol{\beta} \in \mathbb{R}^{p+1 \times r}$ contains constant terms in the first row and coefficients that
 227 weight the contribution of each environmental parameter in the remaining p
 228 rows.

229 The residual error matrix, \mathbf{E} , between identified and predicted natural
 230 frequencies is thus given by

$$\mathbf{E} = \mathbf{Y} - \boldsymbol{\beta}^T \mathbf{Z}^T \quad (3)$$

231 which represents the prediction error of the statistical model. The coefficients
 232 of the statistical model contained in matrix $\boldsymbol{\beta}$ are estimated in a least square
 233 sense by minimizing the norm of \mathbf{E} in a reference training period.

234 Under the assumption that the MLR model is able to reproduce the
 235 part of variance in frequency estimates that is associated with changes in
 236 environmental conditions, quantities contained in the residual error matrix,
 237 $\mathbf{E} \in \mathbb{R}^{r \times N}$, during the monitoring period are unaffected by environmental
 238 parameters and are therefore used for structural health assessment.

239 A damage condition can be identified as an anomaly in the data contained
 240 in matrix \mathbf{E} , under the assumption that damage induces a change in their
 241 distribution. Such anomalies can be detected by the use of control charts
 242 based on properly defined statistical distances: a damage condition is iden-
 243 tified as an outlier in the distribution of the statistical distance. A popular
 244 choice, for instance, is the use of the T^2 -statistic, which is defined as

Mode number	Frequency [Hz]	Damping ratio [%]	Mode Type
1	1.449	1.0	Fx1
2	1.518	1.0	Fy1
3	4.342	1.6	T1
4	4.575	1.1	Fx2
5	4.889	2.3	Fy2
6	7.245	5.1	Fx3
7	7.263	2.7	Fy3

Table 2: Identified modal parameters of the bell tower during the AVT.

$$T^2 = s \cdot (\bar{\mathbf{E}} - \bar{\bar{\mathbf{E}}})^T \cdot \Sigma^{-1} \cdot (\bar{\mathbf{E}} - \bar{\bar{\mathbf{E}}}) \quad (4)$$

245 where s is an integer parameter, referred to as *group averaging size*, $\bar{\mathbf{E}}$ is
246 the mean of the residuals in the subgroup of the last s observations, while
247 $\bar{\bar{\mathbf{E}}}$ and Σ are the mean values and the covariance matrix of the residuals,
248 respectively. Both $\bar{\bar{\mathbf{E}}}$ and Σ are statistically estimated in the same training
249 period used for estimating matrix β in Eq. (3).

250 3. Analysis of hygrothermal effects on natural frequencies

251 3.1. Frequency tracking

252 For the purpose of determining baseline modal parameters of the bell
253 tower, an ambient vibration test (AVT) was carried out on February 16th
254 2015, with the main excitation provided by wind loading. Six high sensi-
255 tivity piezoelectric uni-axial accelerometers of the same type of those used
256 for monitoring (cfr. Section 2.2) were installed on the bell tower. Measure-
257 ment channels are numbered from 1 to 6 in Figure 2. In particular, three
258 accelerometers were located at the base of the cusp and three at the base of
259 the belfry, thus instrumenting both the available floors within the tower.

260 Data were acquired using the same hardware adopted in the monitoring
261 system and modal parameters were extracted from 30-minutes long AVT
262 data using the SSI-data procedure described in Section 2.3. Identified natural
263 frequencies, damping ratios and mode shape types are summarized in Table
264 2. Identified mode shapes are also shown in Fig. 3. Lateral modes are denoted
265 as Fx and Fy, where x and y are the reference axes shown in Figure 2. The
266 third mode is a torsional one and is denoted as T1.

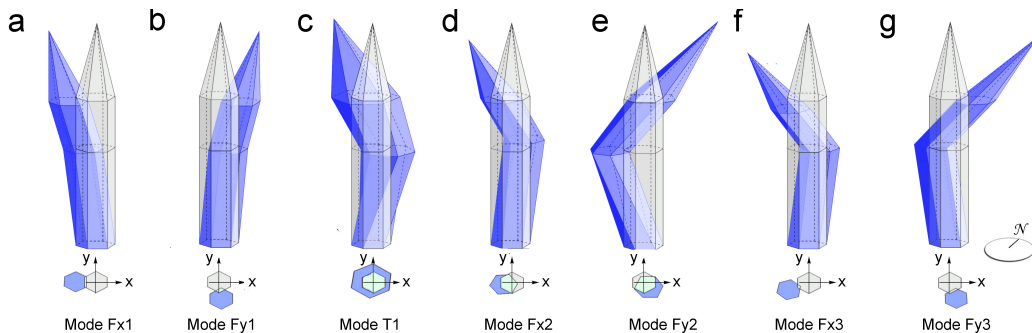


Figure 3: Identified mode shapes of the bell tower during the AVT.

267 The vibration monitoring system has started to continuously acquire ac-
 268 celeration data on December 9th 2014. Since then, time histories of identified
 269 modal parameters are available with a sampling time of 30 minutes, with oc-
 270 casional interruptions when it was necessary to shut down the system in order
 271 to prevent possible damages caused by lightnings hitting the tower during
 272 storms (cfr. Section 2.2).

273 Due to the low levels of vibration of the tower in operational conditions,
 274 some modes are only rarely identified. In particular, modal tracking was
 275 only possible for five modes: the first two bending modes, Fx1 and Fx2,
 276 the first torsional mode, T1, and the second and third bending modes in
 277 the y direction, Fy2 and Fy3, respectively. Fig. 4 shows identified modal
 278 frequencies versus time, where daily fluctuations are clearly apparent and
 279 some seasonal trends are also visible for some modes. As discussed later on,
 280 both daily fluctuations and seasonal trends showed to be essentially related
 281 to temperature variations, while the sharp increase in the frequency of mode
 282 Fy3 observed during the earliest days of 2015 was associated to freezing
 283 conditions.

284 3.2. Correlation analysis

285 Table 3 summarizes the correlation coefficients between environmental
 286 data during the monitoring period. The time history plots of the same en-
 287 vironmental data are depicted in Fig. 5. These results show an overall large
 288 degree of correlation between temperature data recorded by different sensors,
 289 with some temperature measurements that are almost perfectly correlated.
 290 In particular, as also shown in Figure 5, temperatures $T_3 - T_4$, $T_5 - T_6$ and

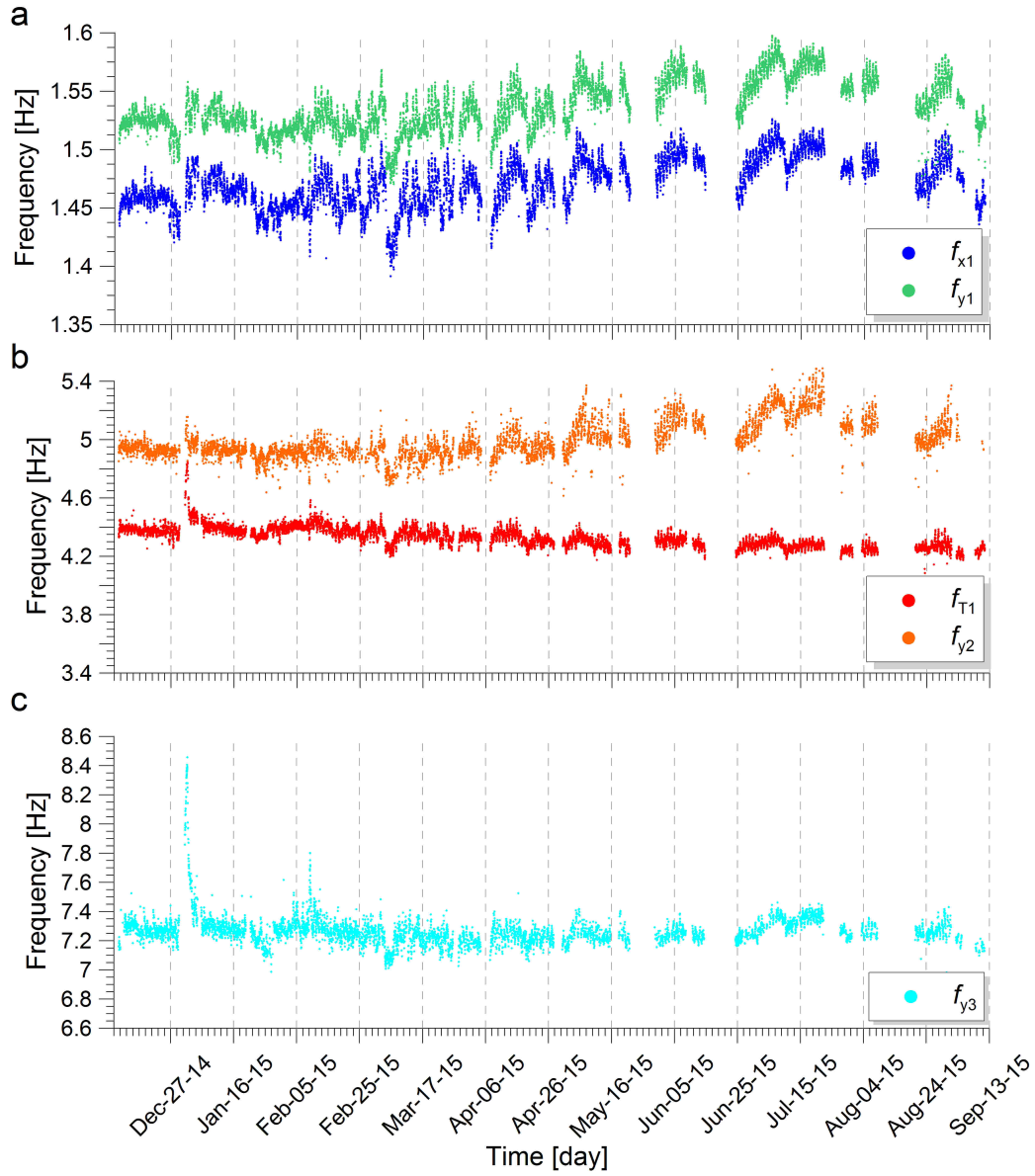


Figure 4: Identified natural frequencies of the bell tower versus time: frequencies of modes f_{x1} and f_{x2} (a); frequencies of modes T and f_{y2} (b); frequency of mode f_{y3} (c).

291 $T_7 - T_8$ are almost coincident, which explains their correlation coefficients
 292 being close to unit values.

293 In general, weaker correlations are observed between outdoor and indoor

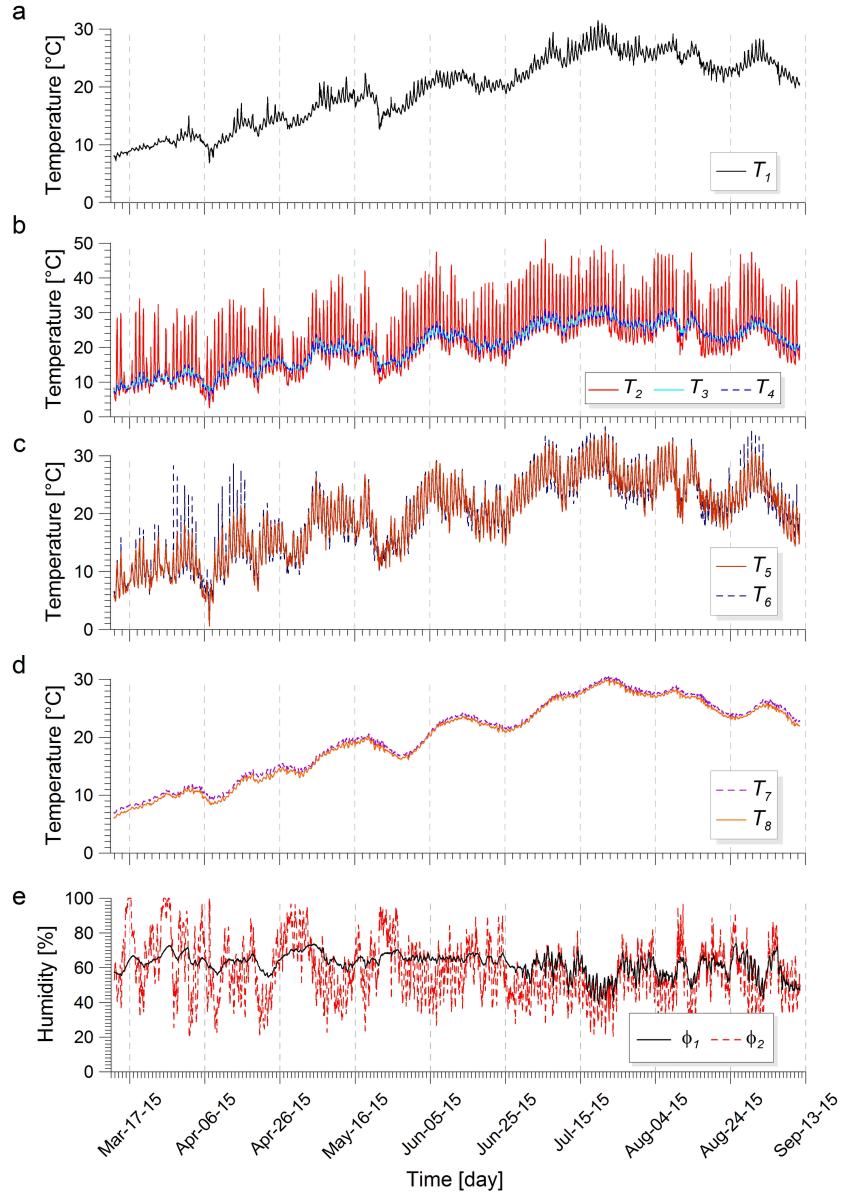


Figure 5: Time history plots of temperature and humidity measurements: T_1 (a); T_2 , T_3 and T_4 (b); T_5 and T_6 (c); T_7 and T_8 (d); ϕ_1 and ϕ_2 (e).

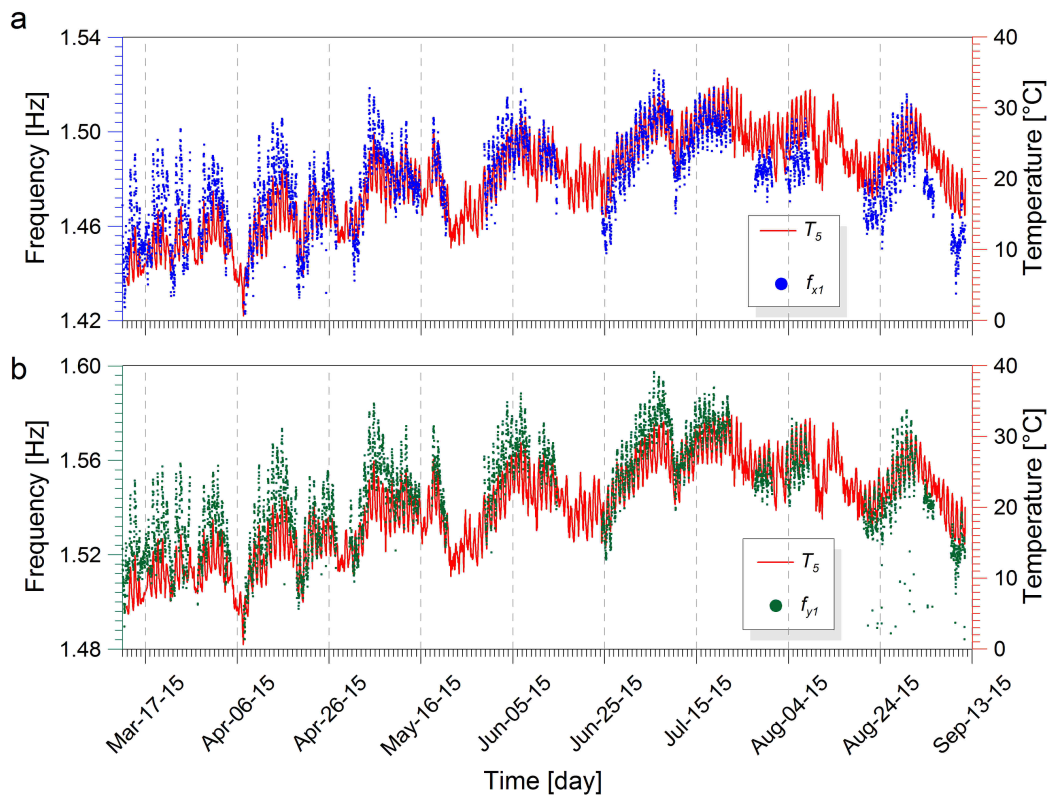


Figure 6: Correlation between frequencies and temperature data: f_{x1} and T_5 (a); f_{y1} and T_5 (b).

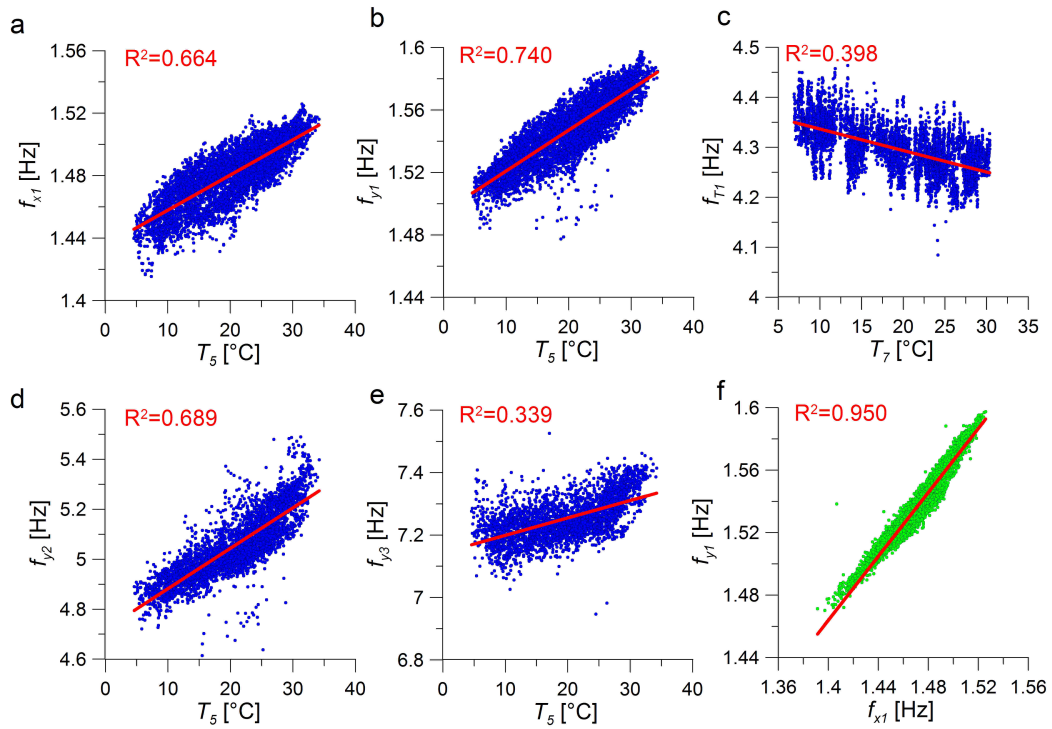


Figure 7: Correlation between frequencies and temperature data (a-e) and resulting correlation between natural frequencies of modes Fx1 and Fy1.

	T_1	T_2	T_3	T_4	T_5	T_6	T_7	T_8	ϕ_1	ϕ_2
T_1	1.00	0.77	0.99	0.98	0.95	0.94	0.99	0.99	-0.40	-0.34
T_2		1.00	0.80	0.82	0.89	0.90	0.71	0.72	-0.33	-0.58
T_3			1.00	1.00	0.97	0.96	0.97	0.97	-0.35	-0.37
T_4				1.00	0.98	0.97	0.96	0.97	-0.34	-0.38
T_5					1.00	0.99	0.91	0.91	-0.32	-0.46
T_6						1.00	0.90	0.91	-0.34	-0.48
T_7							1.00	1.00	-0.39	-0.30
T_8								1.00	-0.38	-0.30
ϕ_1									1.00	0.56
ϕ_2										1.00

Table 3: Correlation coefficients between environmental parameters.

	f_{x1}	f_{y1}	f_{T1}	f_{y2}	f_{y3}
f_{x1}	1.00	0.97	-0.15	0.85	0.31
f_{x2}		1.00	-0.24	0.90	0.29
f_{T1}			1.00	-0.29	0.56
f_{y2}				1.00	0.32
f_{y3}					1.00

Table 4: Correlation coefficients between frequencies.

294 temperature data collected in different positions of the bell tower. In fact,
 295 the construction geometry, affecting the periodical differential solar shading
 296 of the masonry parts and the variable materials and walls' thickness motivate
 297 the local thermal investigation carried out in this work. Just as an exam-
 298 ple, the outdoor temperature T_2 is the one showing the lowest correlation
 299 coefficients with other temperature data, showing that the peculiar and local
 300 construction characteristics affect the differential thermal behavior of such a
 301 complex case study building that should not be neglected in SHM analysis.
 302 A significant difference between indoor and outdoor surface temperatures
 303 is observed owing to the large width of the masonry, which is apparent by
 304 looking at the relatively low correlation between T_2 and T_3 . Indoor surface
 305 and air temperatures within the shaft of the tower are very well correlated
 306 and numerically similar, regardless of the orientation of the sensors, which is
 307 apparent by inspecting the correlation between T_3 and T_4 . The orientation
 308 becomes slightly more important in the case of temperature sensors located
 309 outdoor, due to the effect of solar radiation. Although the correlation be-
 310 tween T_5 and T_6 is very high, differences in peak values are visible in Figure

	T_1	T_2	T_3	T_4	T_5	T_6	T_7	T_8	ϕ_1	ϕ_2
f_{x1}	0.67	0.76	0.75	0.76	0.82	0.80	0.59	0.60	-0.12	-0.39
f_{y1}	0.73	0.78	0.81	0.82	0.86	0.85	0.67	0.68	-0.15	-0.39
f_{T1}	-0.57	-0.22	-0.50	-0.48	-0.41	-0.41	-0.63	-0.62	0.18	0.00
f_{y2}	0.76	0.75	0.81	0.82	0.83	0.83	0.71	0.72	-0.35	-0.47
f_{y3}	0.53	0.54	0.57	0.57	0.58	0.58	0.49	0.50	-0.35	-0.32

Table 5: Correlation coefficients between frequencies and environmental parameters.

311 5. One last observation concerns air temperature within the cusp, which is
312 seen to undergo very small daily fluctuations conceivably because of the high
313 transmittance and low thermal capacity of the roof of the tower.

314 Correlation coefficients between temperature data and air humidity are
315 remarkably low and negative in sign, due to a decrease in relative air humidity
316 with increasing air temperature.

317 Correlation coefficients between natural frequencies are summarized in
318 Table 4. These results generally show a high degree of correlation between
319 the natural frequencies of modes F_{x1} , F_{y1} and F_{y2} . The torsional mode, $T1$
320 exhibits a significant correlation only with mode F_{y3} that, in turn, is only
321 slightly correlated with other modes.

322 The reason for the high degree of statistical correlation between natu-
323 ral frequencies is imputable to their dependency on environmental parame-
324 ters. Table 5 summarizes such correlations highlighting, in particular, that
325 all frequencies, with the exception of f_{T1} , exhibit positive correlation coeffi-
326 cients with temperature profiles, indicating therefore an increase in natural
327 frequency with increasing temperature, in agreement with other literature
328 works and conceivably attributable to closing of micro-cracks within mortar
329 layers due to thermal expansion [6, 7]. The negative correlations between
330 f_{T1} and temperature data is worth noting and it is here attributed to the
331 thermally-induced slackening of tie elements and of fiber reinforcements in-
332 stalled during the retrofit of 2002 (cfr. Section 2.1), reducing the lateral
333 confinement and thus determining a softening effect on the dynamic behav-
334 ior of the tower. Another remark on the results is that, with the exception of
335 mode $T1$, temperature T_5 is the environmental parameter that corresponds
336 to the largest correlations with natural frequencies. It is, therefore, placed
337 in the best location for an effective removal of environmental effects from
338 natural frequencies.

339 Figure 6 shows superimposed time history plots of natural frequencies and

f_i	T_{s_i}	$f_{i,0}$ (Hz)	$\kappa_{i,T}$ (mHz/°C)
f_{x1}	T_5	1.435	2.25
f_{y1}	T_5	1.495	2.61
f_{T1}	T_7	4.380	-4.31
f_{y2}	T_5	4.721	16.17
f_{y3}	T_5	7.143	5.58

Table 6: Parameters of best fitting lines between frequencies and temperature data.

340 temperature data, considering the frequencies of the first two bending modes
341 and temperature data T_5 . These plots visually emphasize the frequency-
342 temperature correlations, showing in particular that daily fluctuations of
343 natural frequencies are determined by daily fluctuations of temperature and
344 that long-term increments of natural frequencies during the monitoring pe-
345 riod are determined by seasonal increments in temperature.

346 Figure 7 shows plots of natural frequencies against the temperature data
347 for which they exhibit the maximum absolute values of the correlation coeffi-
348 cients. These plots show that frequency-temperature correlations are almost
349 linear, as confirmed by the relatively high values of the coefficient of deter-
350 mination, R^2 , obtained through best fitting linear trends. The best fitting
351 lines in Figure 7 have the following general equation:

$$f_i = f_{i,0} + \kappa_{i,T} T_{s_i} \quad (5)$$

352 where $i = x_1, x_2, T, y_2, y_3$ indicates the mode, s_i is the number of the temper-
353 ature sensor corresponding the largest absolute correlation coefficient with
354 f_i , while $f_{i,0}$ and $\kappa_{i,T}$ are frequency at 0 °C and frequency-temperature sensi-
355 tivity coefficients, respectively, whose least square estimates are summarized
356 in Table 6. The relatively high values of $\kappa_{i,T}$ demonstrate the significant
357 variations of natural frequencies with temperature. In particular, it should
358 be noticed that, according to the results reported in Table 6, a temperature
359 change of 10 °C produces relative changes in natural frequencies between 0.8
360 and 3.4%, which can be considered as large in comparison with changes in
361 natural frequencies typically produced by small damages in full-scale struc-
362 tures [22].

363 Correlations between frequencies and relative humidity data, in Table 5,
364 also deserve some attention. In particular, the negative correlations between
365 natural frequencies and humidities, with the only exception of mode $T1$,
366 could be interpreted in light of the negative correlations between humidity

367 and temperature, as well as to a slight mass increment due to moisture in
368 the masonry. However, correlations observed in this work are too weak to
369 reliably conclude about the physical mechanisms governing humidity effects
370 on natural frequencies.

371 *3.3. Freezing conditions*

372 Sudden increases in natural frequencies of the bell tower were observed
373 during the earliest days of 2015. This happened before implementing the
374 environmental monitoring hardware described in Section 2.2. In order to
375 properly interpret this behavior, frequencies identified during those days
376 have been inspected in relation to temperature data recorded from a nearby
377 weather monitoring station located in the historical center of Perugia. Re-
378 sults are shown in Figure 8 and clearly demonstrate that the increases in
379 natural frequencies occurred during three consecutive freezing days, in which
380 temperature was steadily below 0 °C. In particular, natural frequencies in-
381 creased in time for the whole freezing period, while started to decrease and
382 to recover the original values right after temperature raised over 0 °C.

383 The results showed in Figure 8, although not permitting a significant
384 statistical analysis, clearly demonstrate that frequency-temperature correla-
385 tions drastically change in freezing conditions. Contrarily to what observed in
386 above 0 °C conditions, frequencies below 0 °C increase with decreasing tem-
387 perature. This circumstance is conceivably caused by the stiffening effect
388 produced by ice forming within the micro-pores of the masonry. Resulting
389 variations in natural frequencies seem to be progressively more significant in
390 higher order modes, which might be related to faster freezing of the belfry
391 with respect to the shaft. The case of the third bending mode in the y di-
392 rection, mode $Fy3$, is especially noteworthy in Figure 8: its frequency, in a
393 continuously freezing time period of about three days, exhibited a remark-
394 able increase of about 20%, that roughly corresponds to a 40% increase in
395 structural stiffness.

396 **4. Statistical reconstruction of natural frequencies**

397 *4.1. Effect of training data on prediction errors*

398 As discussed in Section 2.4, natural frequencies can be independently es-
399 timated using environmental parameters as predictors of MLR models, Eq.
400 (2). The use of linear statistical models is in this case supported by the

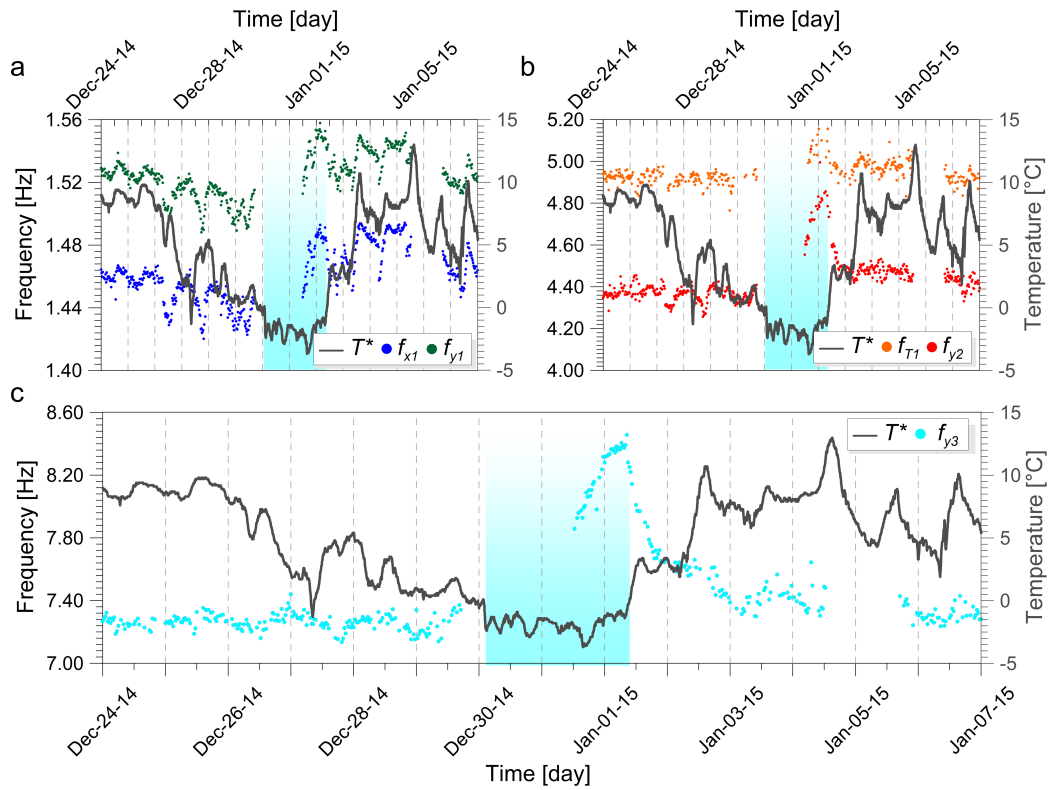


Figure 8: Time history plots of identified natural frequencies and temperature data between December 24th 2014 and January 8th 2015 (the area in blue indicates the period with temperature below 0 C): time histories of f_{x1} and f_{y1} (a); time histories of f_{T1} and f_{y2} (b); time history of f_{y3} (c).

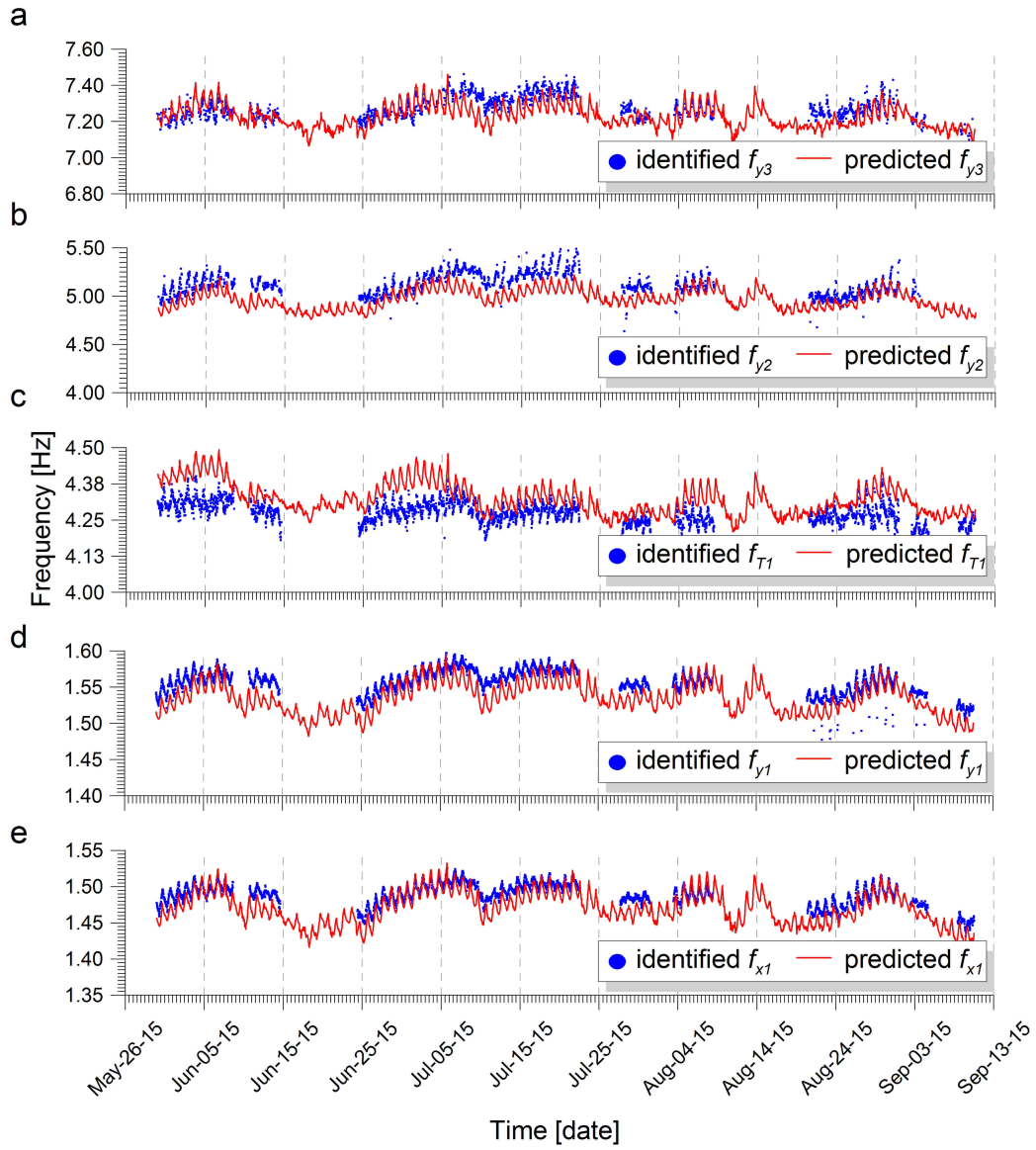


Figure 9: Identified and statistically predicted natural frequencies.

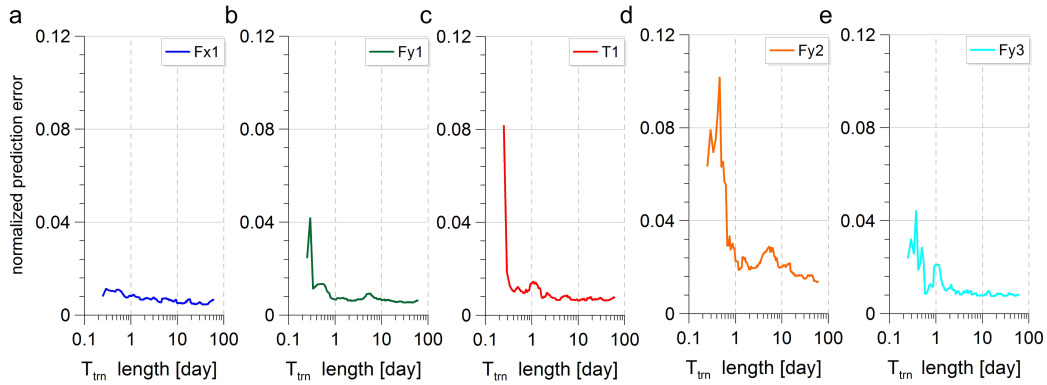


Figure 10: Normalized prediction error of MLR model versus training period length: mode Fx1 (a); mode Fy1 (b); mode T (c); mode Fy2 (d); mode Fy3 (e).

401 observed linearity of the correlations between natural frequencies and tem-
 402 perature data.

403 In order to obtain accurate frequency predictions, it is necessary to es-
 404 timate the coefficients of MLR models using data recorded in a sufficiently
 405 long training period. As an example, Figure 9 shows identified and predicted
 406 frequencies in the observation period, using a training period of sixty days
 407 and using all available environmental monitoring sensors. The good quality
 408 of the statistical reconstruction of the frequencies is apparent, especially for
 409 low order modes.

410 The effect of a change in the length of the training period on the prediction
 411 error of the statistical model is investigated in Figure 10. For each mode,
 412 the error is computed as the root mean square of the difference between
 413 identified and predicted natural frequency values, normalized by the variance
 414 of the identified natural frequency values. The error is computed in the same
 415 observation period of 65 days following the longest training period of 60 days.
 416 The results show that statistical models' accuracy stabilizes very quickly after
 417 about 10 days. The residual error after proper training represents the part of
 418 variance in identified frequencies that is not related to environmental effects,
 419 while it is essentially determined by random errors in output only modal
 420 identification.

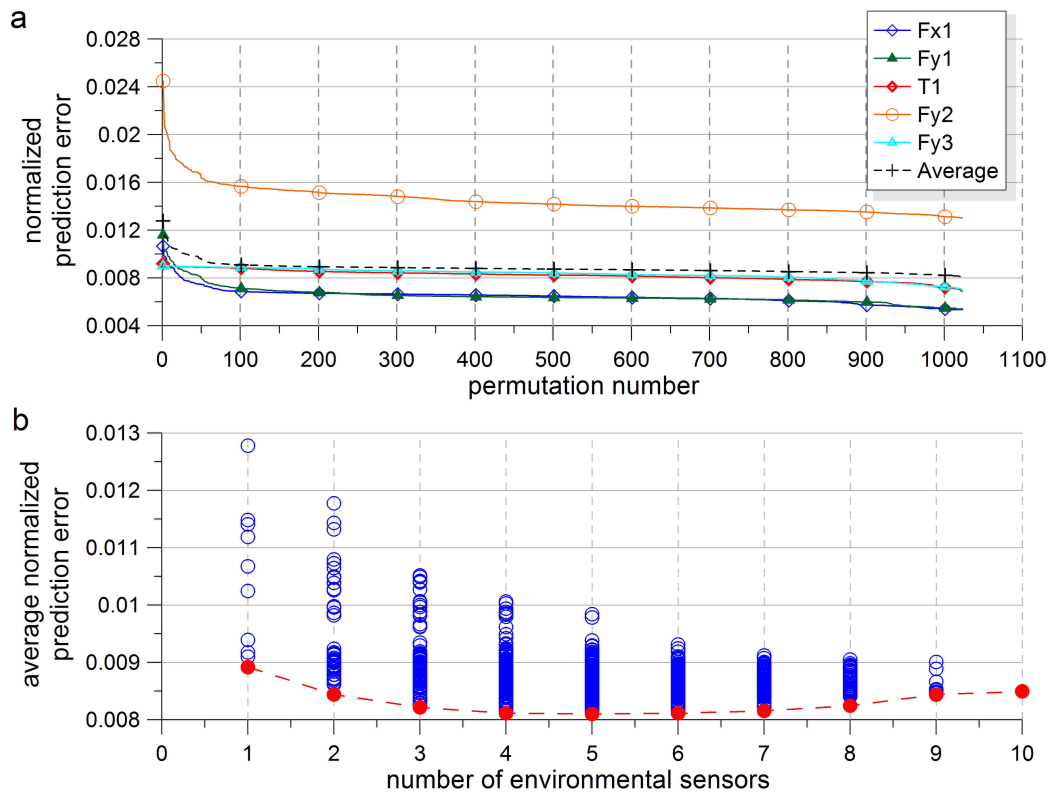


Figure 11: Prediction accuracy with all possible permutations of environmental monitoring sensors: prediction errors sorted in descending order (a); average normalized prediction error versus number of sensors (b).

No. of sensors	Error	Optimal layout
1	8.917e-3	$[T_5]$
2	8.439e-3	$[T_1 \ T_4]$
3	8.214e-3	$[T_5 \ T_7 \ T_8]$
4	8.111e-3	$[T_1 \ T_4 \ T_5 \ \phi_1]$
5	8.100e-3	$[T_1 \ T_3 \ T_4 \ T_5 \ \phi_1]$
6	8.110e-3	$[T_1 \ T_3 \ T_4 \ T_5 \ T_6 \ \phi_1]$
7	8.154e-3	$[T_1 \ T_3 \ T_4 \ T_5 \ T_6 \ \phi_1 \ \phi_2]$
8	8.244e-3	$[T_1 \ T_2 \ T_3 \ T_4 \ T_5 \ T_6 \ \phi_1 \ \phi_2]$
9	8.437e-3	$[T_1 \ T_3 \ T_4 \ T_5 \ T_6 \ T_7 \ T_8 \ \phi_1 \ \phi_2]$
10	8.492e-3	$[T_1 \ T_2 \ T_3 \ T_4 \ T_5 \ T_6 \ T_7 \ T_8 \ \phi_1 \ \phi_2]$

Table 7: Optimal environmental sensors' layouts for natural frequency prediction.

421 *4.2. Optimal layout of hygrothermal monitoring sensors*

422 A major aspect to be considered in practical applications is limiting the
423 number of monitoring sensors of ambient relative humidity, dry bulb and
424 masonry superficial temperature to what strictly necessary to achieve good
425 frequency estimates. In order to investigate this aspect for the considered
426 case study, Figure 11 shows the evolution of normalized prediction errors
427 in all of the 1023 possible sensors' layouts using some or all of the 10 en-
428 vironmental sensors considered in this paper. The error is computed as in
429 the case of Figure 10 and the average error is computed by considering all
430 five continuously identified modes. The optimal sensors layouts for varying
431 number of sensors are summarized in Table 7.

432 The presented results show that one single optimally located sensor can
433 be sufficient to achieve about 90% of the accuracy that can be achieved with
434 more than one sensor. In the present case, the optimal sensor is T_5 as it is the
435 one exhibiting the largest correlations with natural frequencies. By increasing
436 the number of predictors, the accuracy improves if the sensors' are deployed
437 in different locations along the tower, in such a way to consider different
438 portions of the structure and different exposures to environmental forcing.
439 In general, air temperature sensors seem to be more informative than surface
440 temperature sensors and the best statistical prediction accuracy is achieved
441 with five sensors, while further enlarging the number of sensors can be even
442 detrimental. Humidity starts to play a significant role if coupled with at least
443 three temperature sensors but it is necessary to attain the best prediction
444 accuracy.

445 5. Conclusions

446 The paper has investigated the effects of changes in environmental con-
447 ditions on the natural frequencies of a continuously monitored monumen-
448 tal masonry bell tower. The topic is relevant for vibration-based structural
449 health monitoring using natural frequencies as damage sensitive features.

450 The results have shown that dry bulb temperature variations can produce
451 significant changes in natural frequencies, up to 16 mHz/°C, while effects of
452 air humidity are relatively marginal.

453 Three temperature-driven types of frequency variation phenomena have
454 been observed. The first one is the increase in the eigenfrequencies of bend-
455 ing modes with increasing temperature, due to thermal expansion in the
456 masonry determining closing of micro-cracks in mortar layers, which was al-
457 ready observed in other literature works. The second one is the decrease of
458 torsional eigenfrequencies with increasing temperature, which is attributed
459 to thermally-induced slackening of tie elements and of fiber reinforcements.
460 The third one is the increase in natural frequencies with decreasing tem-
461 perature which occurs in freezing conditions due to ice forming within the
462 micro-pores of the masonry.

463 When continuously identified natural frequencies are used for structural
464 health assessment purposes, temperature effects need to be carefully removed.
465 Results presented in this paper show that multivariate linear regressions are
466 effective for this purpose, as statistical correlations between frequencies and
467 temperature are remarkably linear.

468 The optimal statistical reconstruction of natural frequencies of the mon-
469 itored tower required the use of four temperature sensors (air and surface
470 thermal measurements) and one humidity sensor, located at different heights
471 and in different regions of the tower characterized by similar material and
472 geometrical characteristics but different environmental exposure to solar ra-
473 diation, winds, etc. However, one optimally located air temperature sensor
474 with a Southward exposure was found sufficient to achieve about 90% of the
475 statistical prediction accuracy that was achieved with more than one sensor.
476 In general, the accuracy of such reconstruction increases with the length of
477 the training period, but a very fast convergence was evidenced, which indi-
478 cated that about 10 days of training period were already sufficient to gain
479 relatively accurate predictions.

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497

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